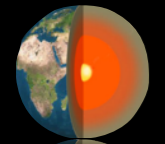
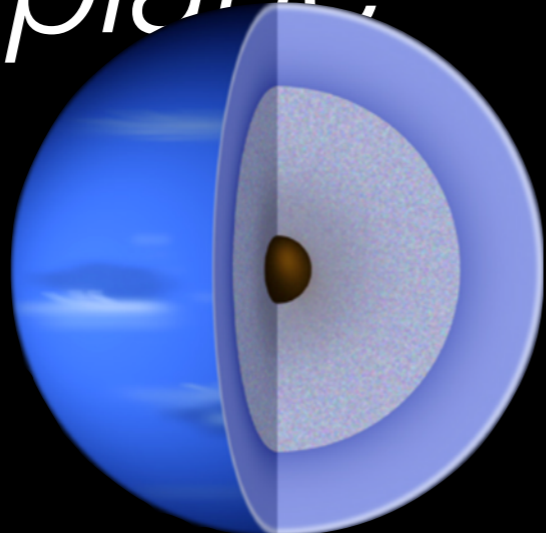
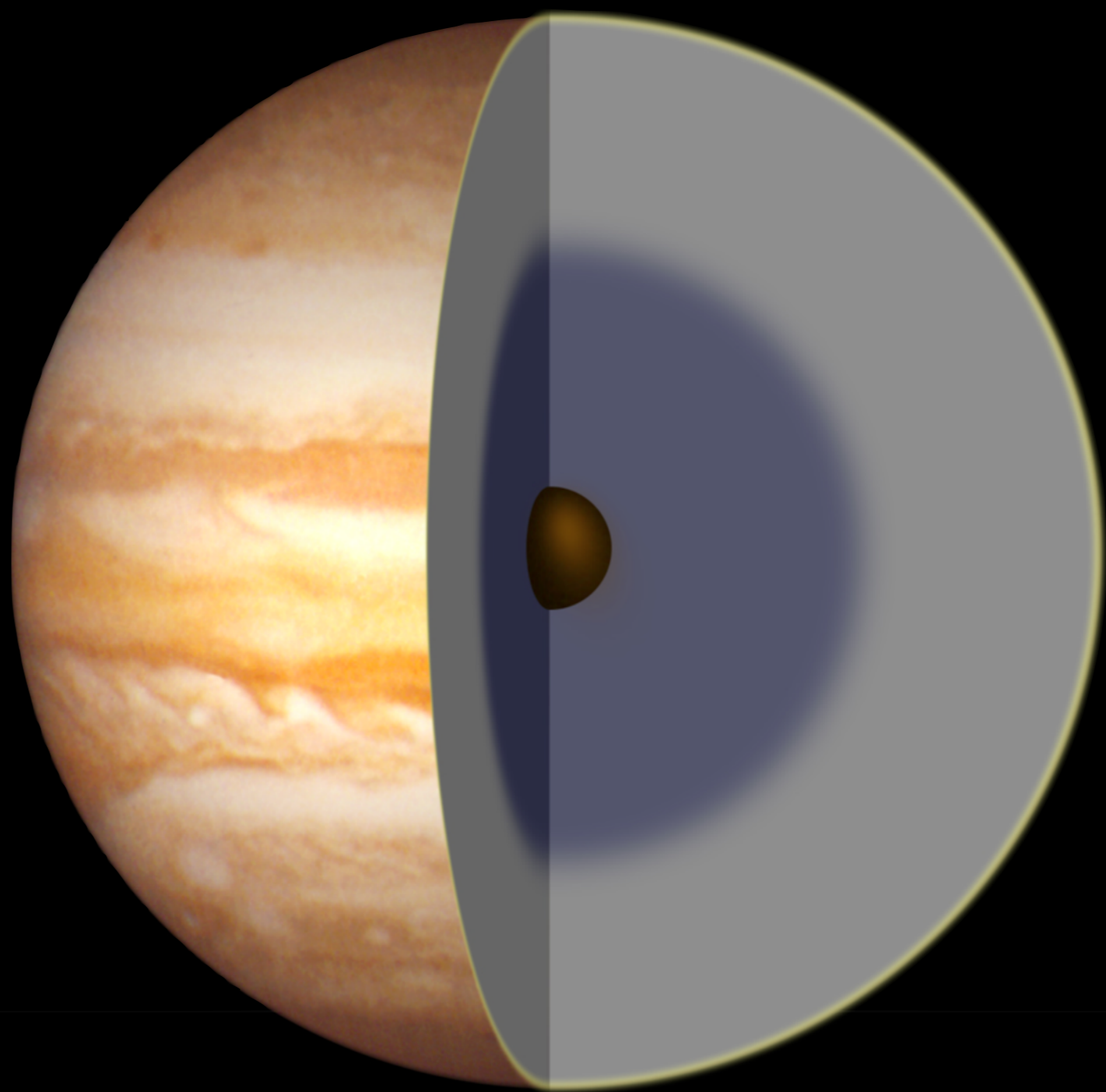
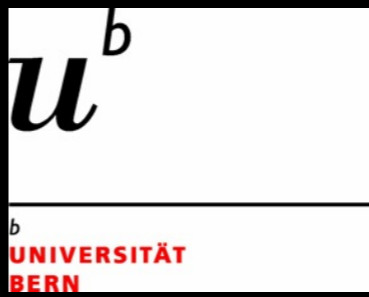


# *Breaking the compositional degeneracy in the a-M-R-t plane*



Christoph Mordasini

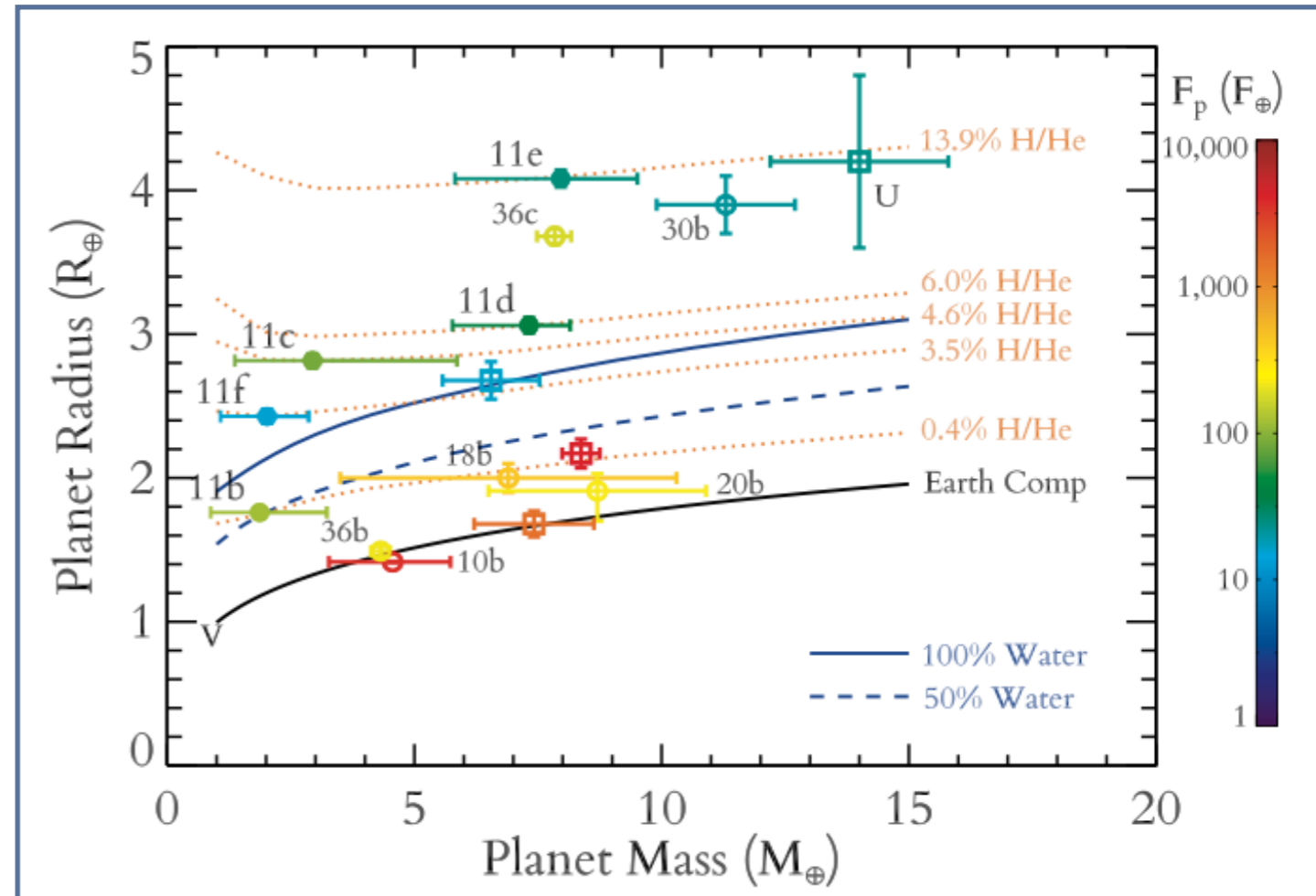
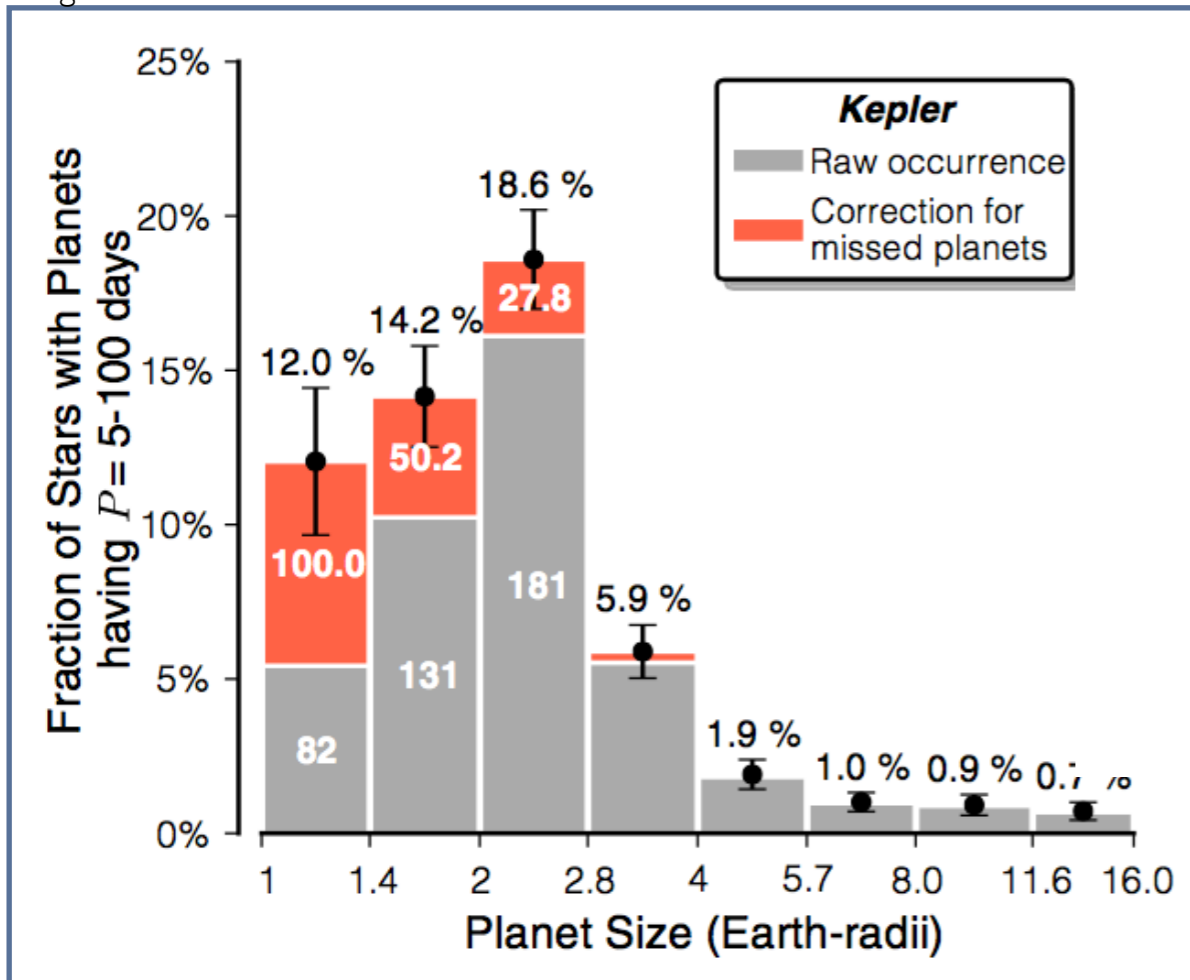
Y. Alibert, W. Benz, K. Dittkrist, P. Molliere, S. Jin, G. Marleau



# Close-in low-mass planets

Petigura et al. 2013

Lissauer et al. 2013



- Very frequent: ~50% of solar like star ( $1 < R/R_{\oplus} < 4$  &  $P < 100$  days; Kepler)
- From RV: ~40% with  $M < 30 M_{\oplus}$  inside 50 days (HARPS)
- Large diversity in composition. Some w. low density (H/He envelopes of ~1-10% for  $R/R_{\oplus} > 1.6$ ), some Earth-like

*Formation mechanism?*



# Formation mechanism?

	Strictly in situ	Migration then final assembly	Large scale migration after assembly from $a > a$
Core composition	Rocky	Rocky - Icy potentially radial composition gradient	Icy
Primordial H/He (post-formation)	Yes (w/o isolation) No (w isolation)	Yes (w/o isolation) No (w isolation)	Yes

Knowing the bulk composition (H/He; rocky, icy, mixed) would be of very high interest for formation theory

Formation beyond iceline: ice mass fraction 50-75%

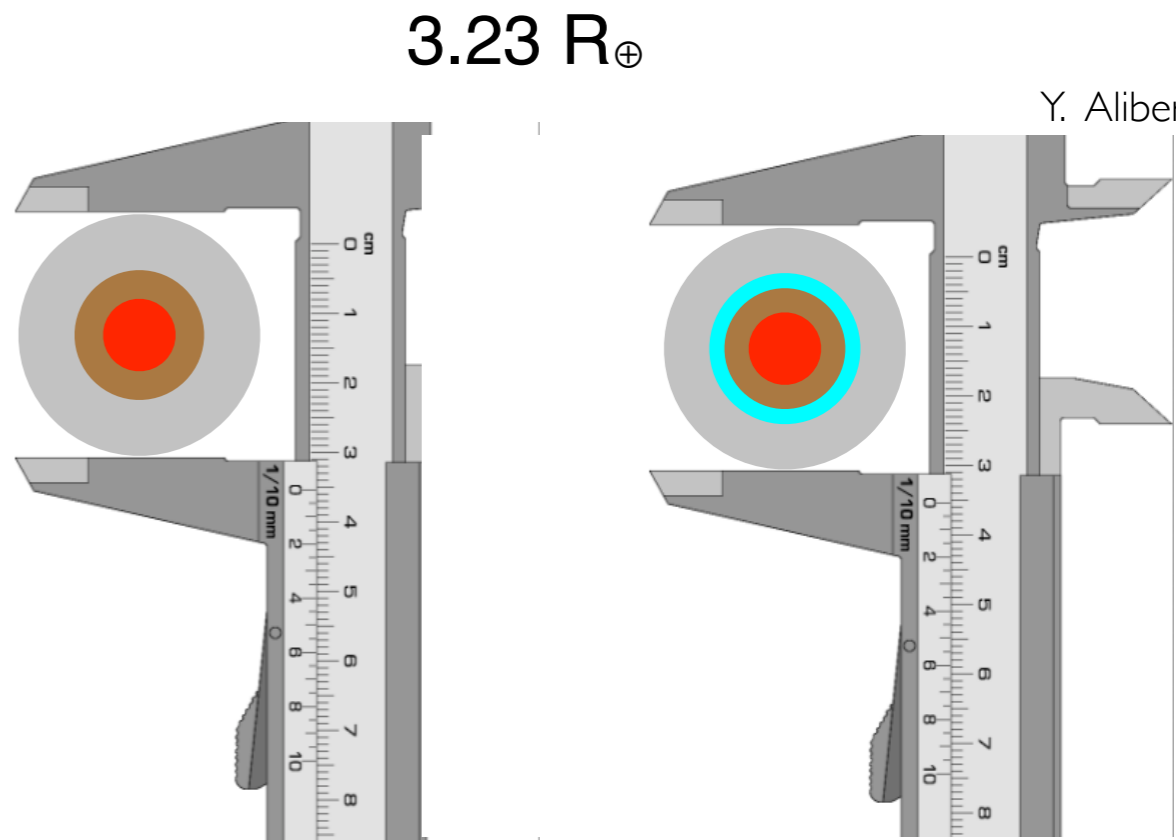
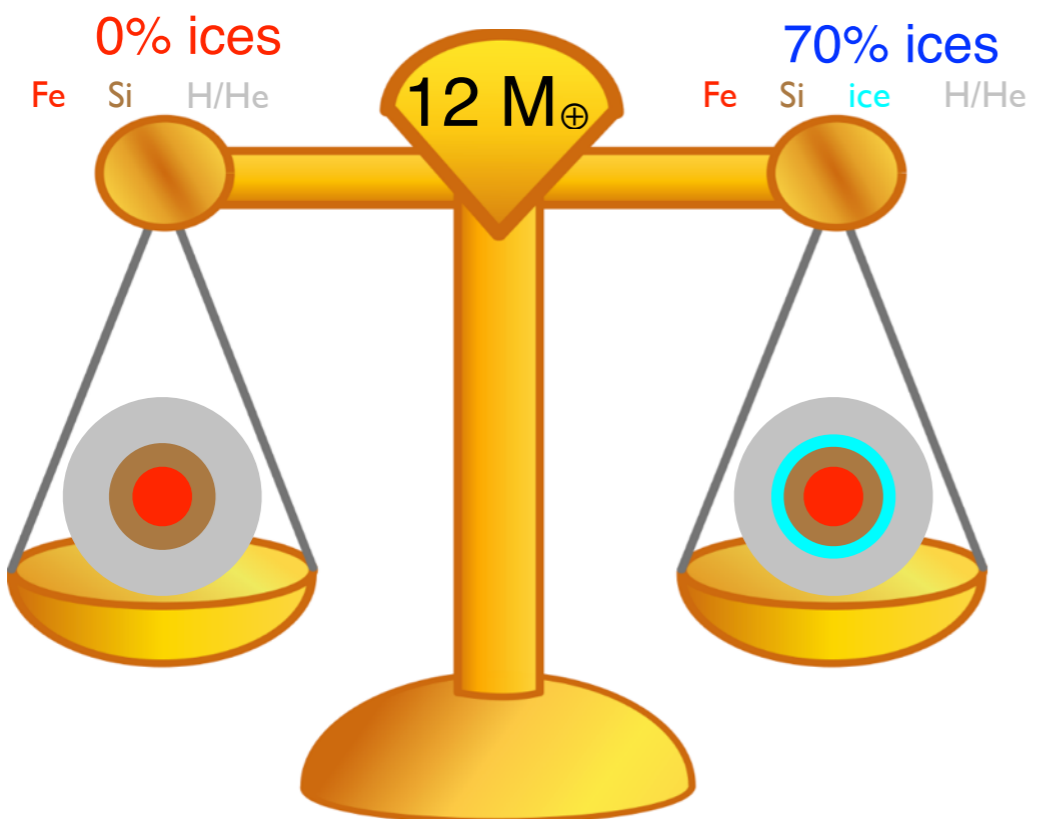


# Degenerate M-R relation

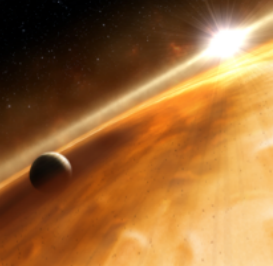
Formation of close-in low-mass planets: in situ vs. migration  
Formation beyond iceline: ice mass fraction 50-75%

Knowing the bulk composition (H/He; rocky, icy, mixed) would be of very high interest for formation theory

Even for only the 4 standard “ingredients” of planetary interiors (iron, silicates, ices, H/He) the M-R is degenerate:

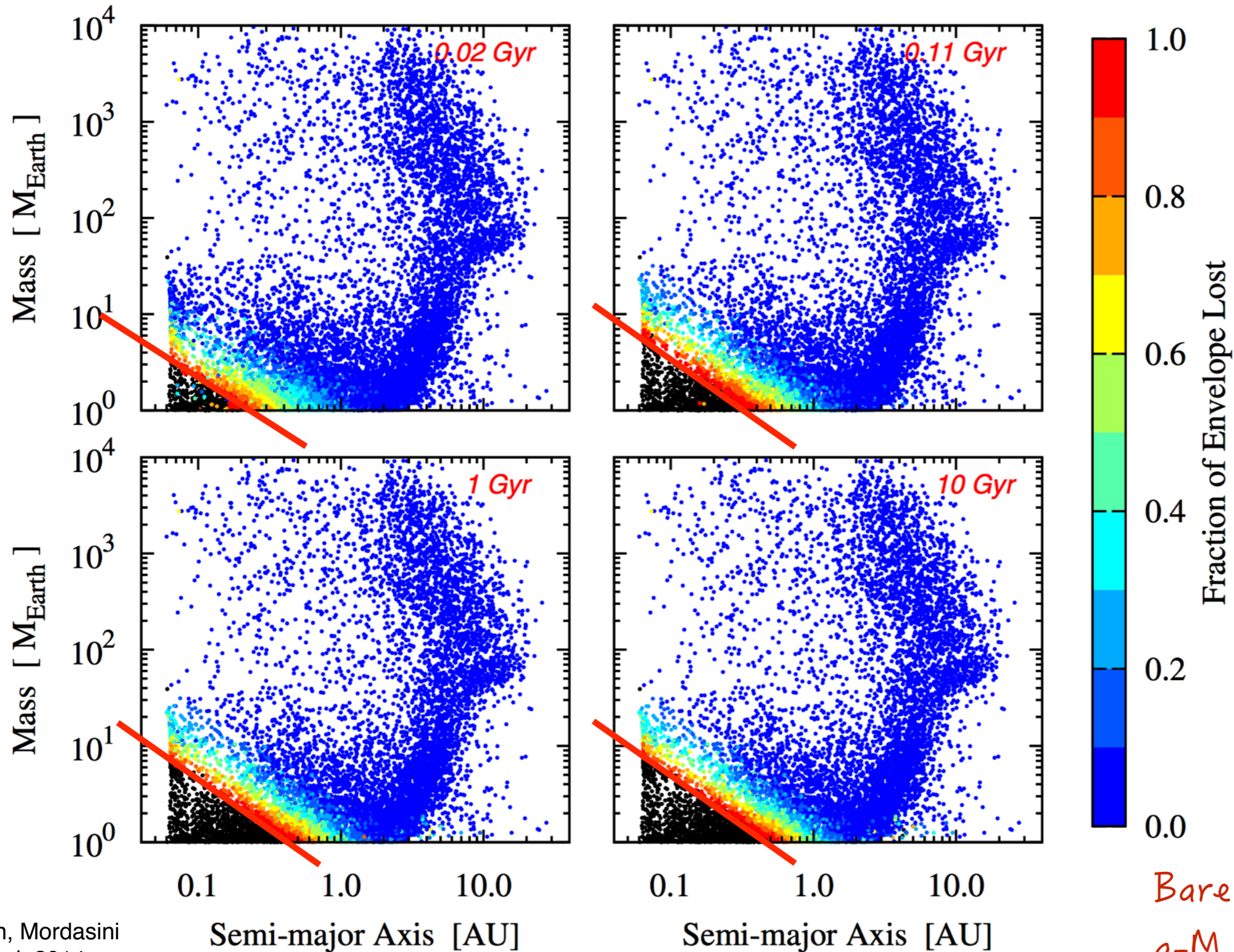


⇒ reduce the number of unknown “ingredients” to 2 for some planets



# H/He: Evolution with atmo. escape

$M_{\text{star}}=1 M_{\text{sun}}$  Isothermal Type I rate x 0.1. Cold accretion. 1 embryo/disk,  $f_{\text{opa}}=0.003$

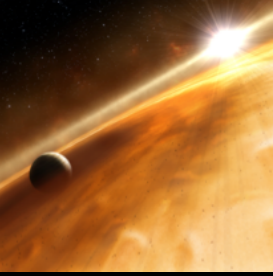


Bern model:  
Core-accretion  
population  
synthesis

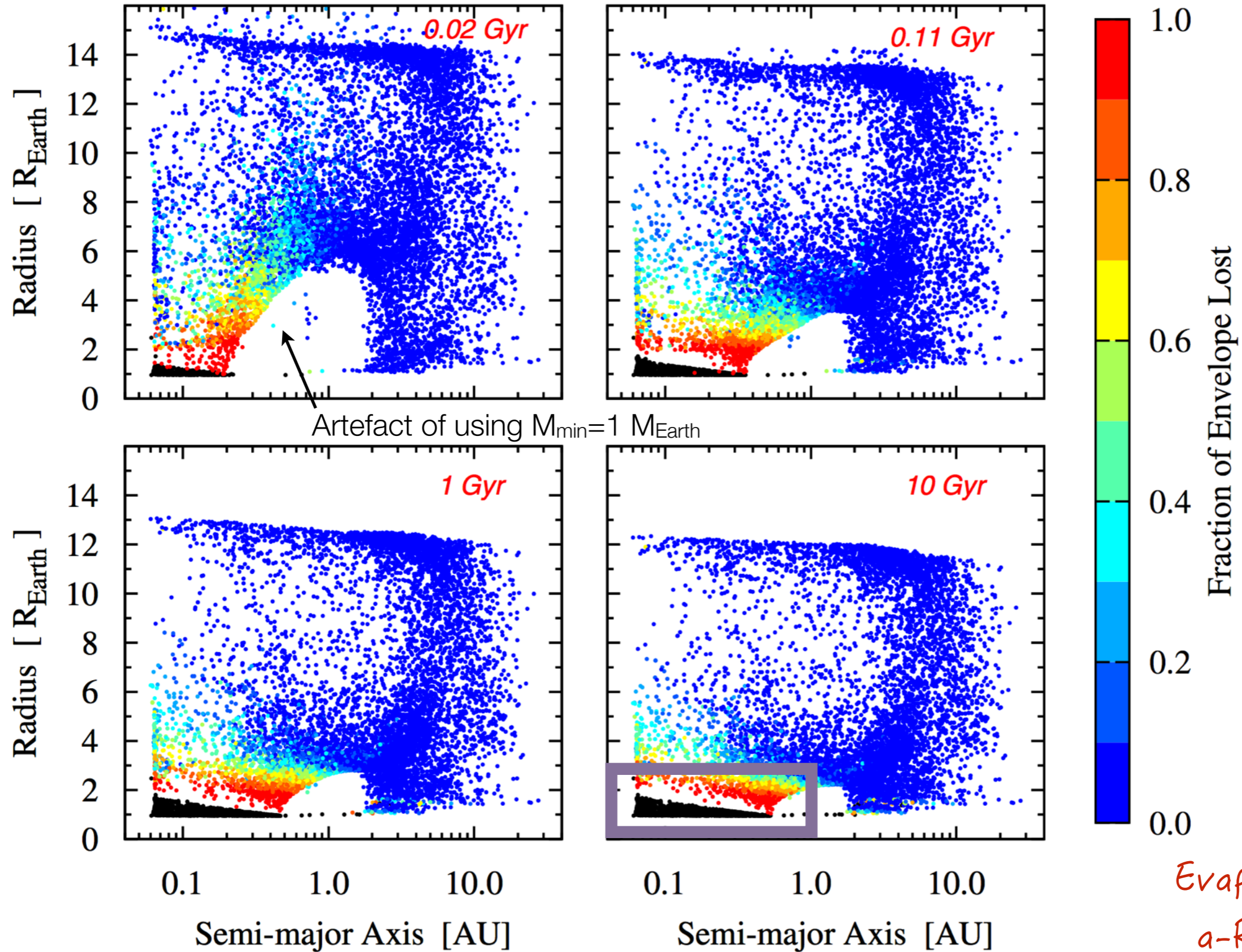
Self-consistent  
formation and  
evolution (cont.  
& cooling) with  
XUV-driven  
atmo. escape.

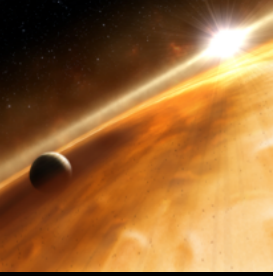
Not much  
evolution after  
> ~100 Myr

*Bare core triangle  
a-M is hardly affected*



# The evaporation valley



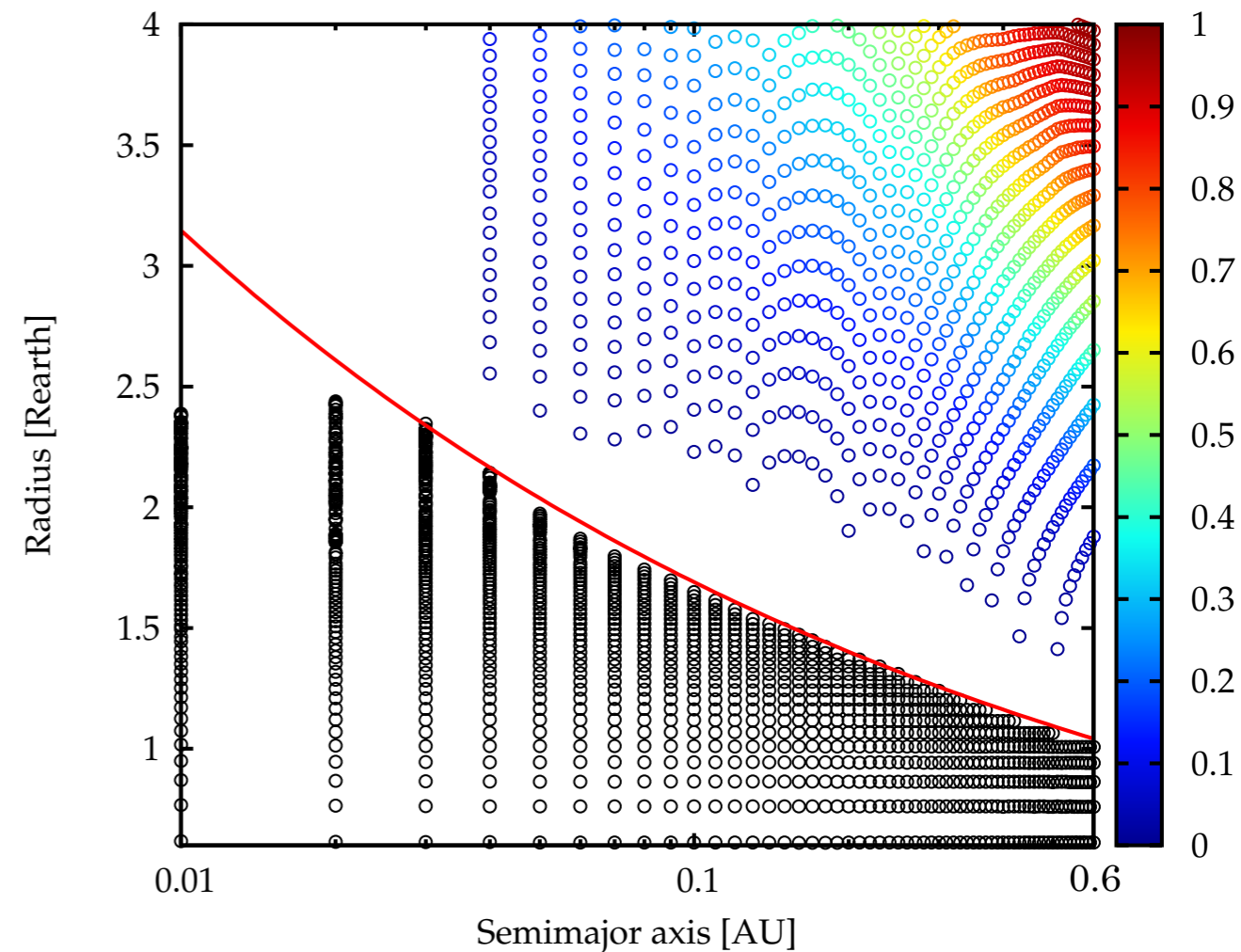
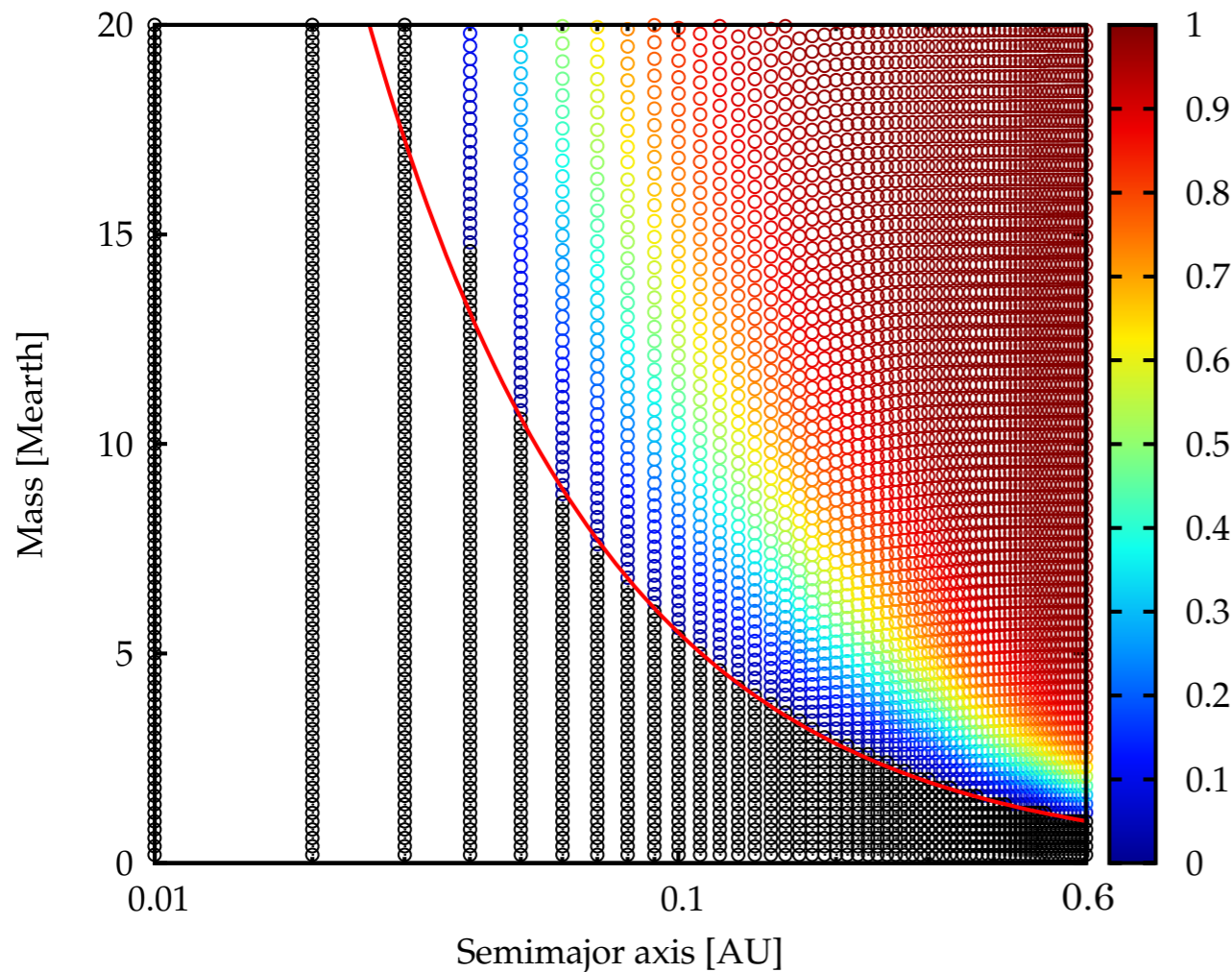


# Systematic investigation

Systematic study:  $a=0.01-0.6$  AU;  $M_{\text{core}}=0.2-20 M_{\text{Earth}}$

Initial H/He envelope mass:  $M_{\text{enve}} = 0.03 \times \left(\frac{M_{\text{core}}}{M_{\oplus}}\right)^2 M_{\oplus}$

**T=5 Gyrs**



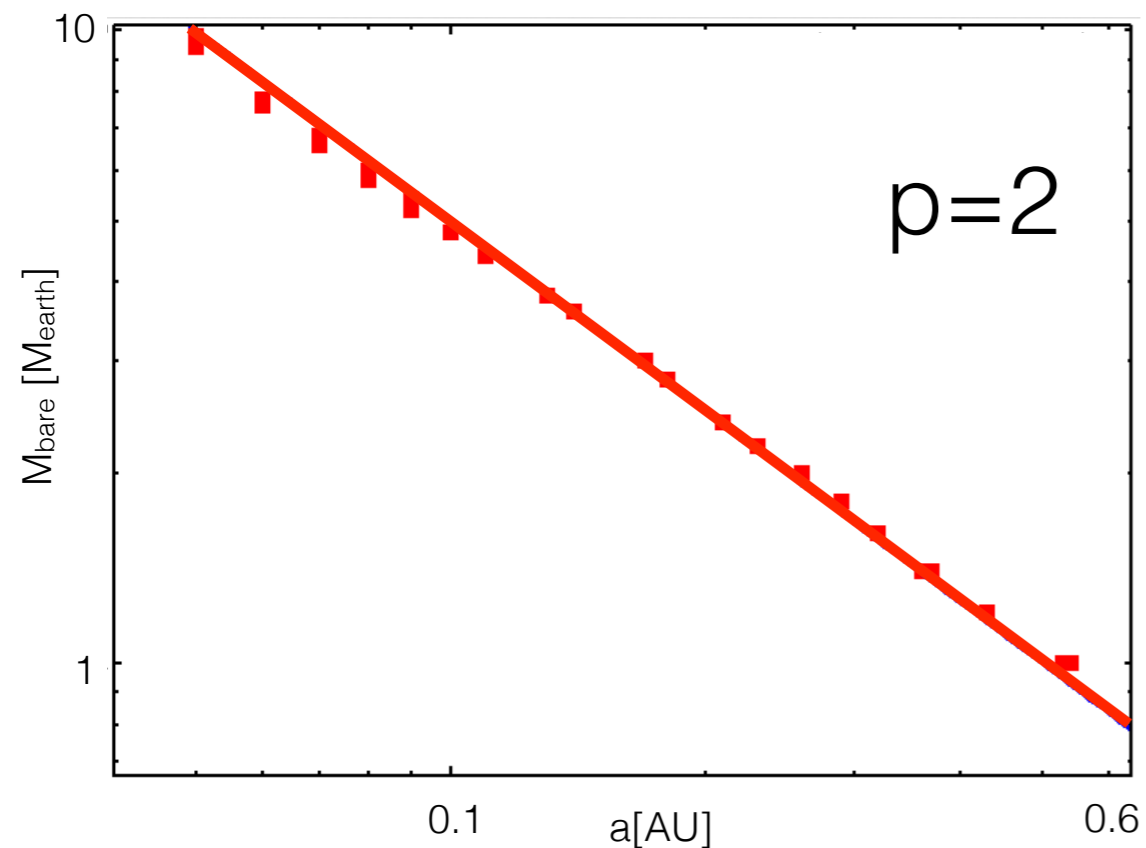
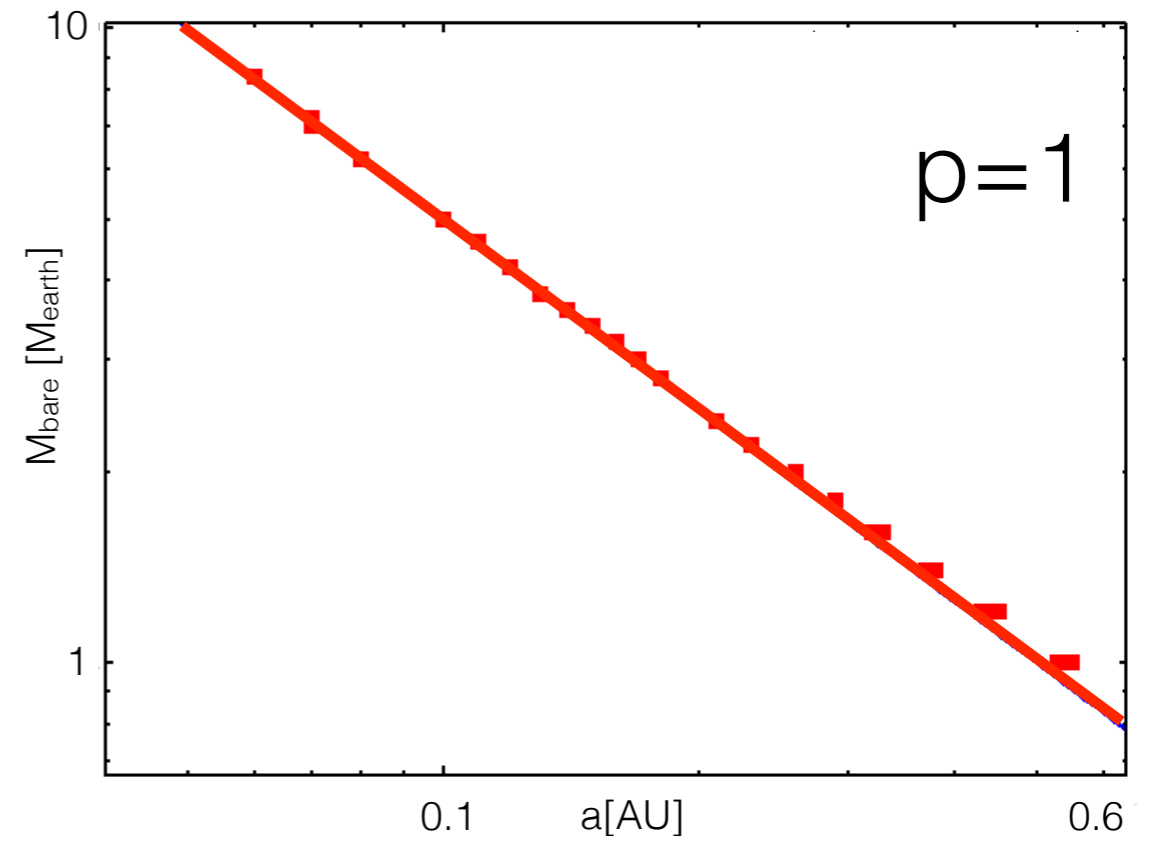
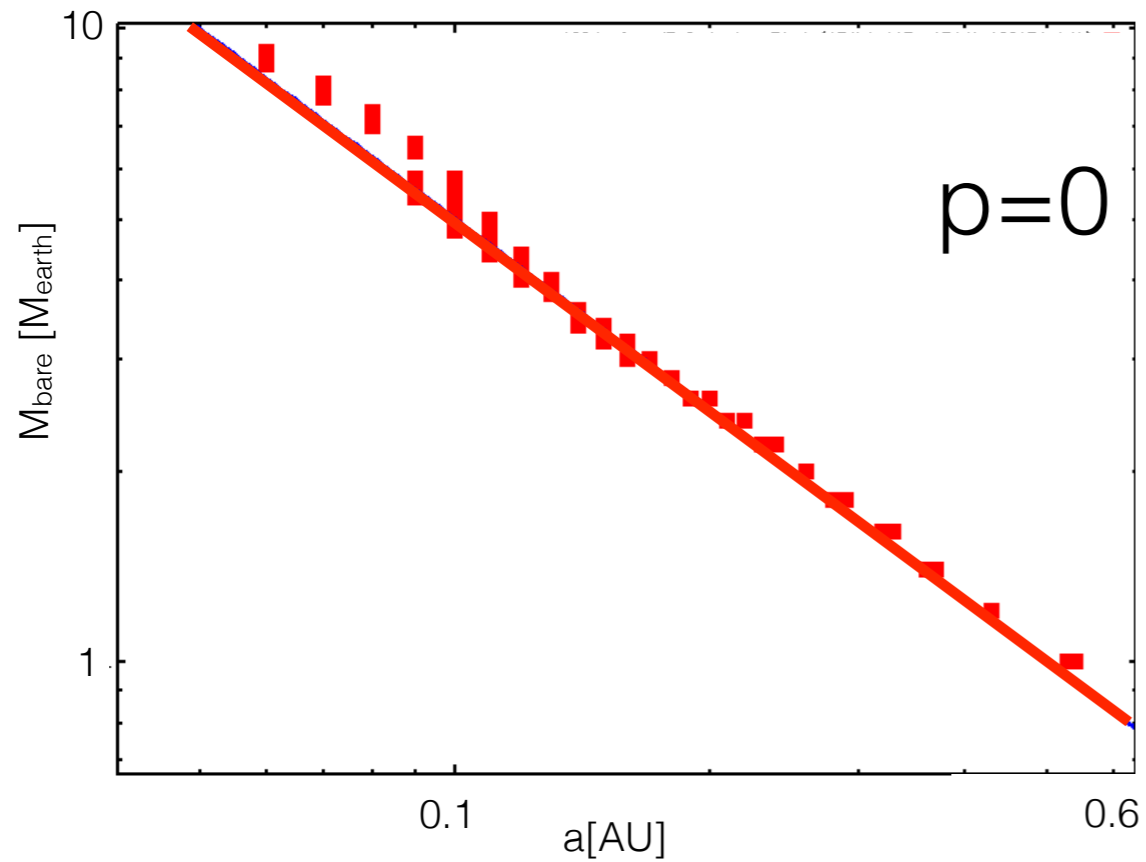
$$\frac{M_{\text{bare}}}{M_{\oplus}} = 5.5 \left(\frac{a}{0.1\text{AU}}\right)^{-0.95}$$

$$\frac{R_{\text{bare}}}{R_{\oplus}} = 1.69 \left(\frac{a}{0.1\text{AU}}\right)^{-0.27}$$

*cf. Rogers 2014*



# The solid-gas transition



$$M_{\text{enve}} = 0.03 \times \left( \frac{M_{\text{core}}}{M_{\oplus}} \right)^p M_{\oplus}$$

*$M_{\text{bare}}$  independent on  $p$*

*Why?*

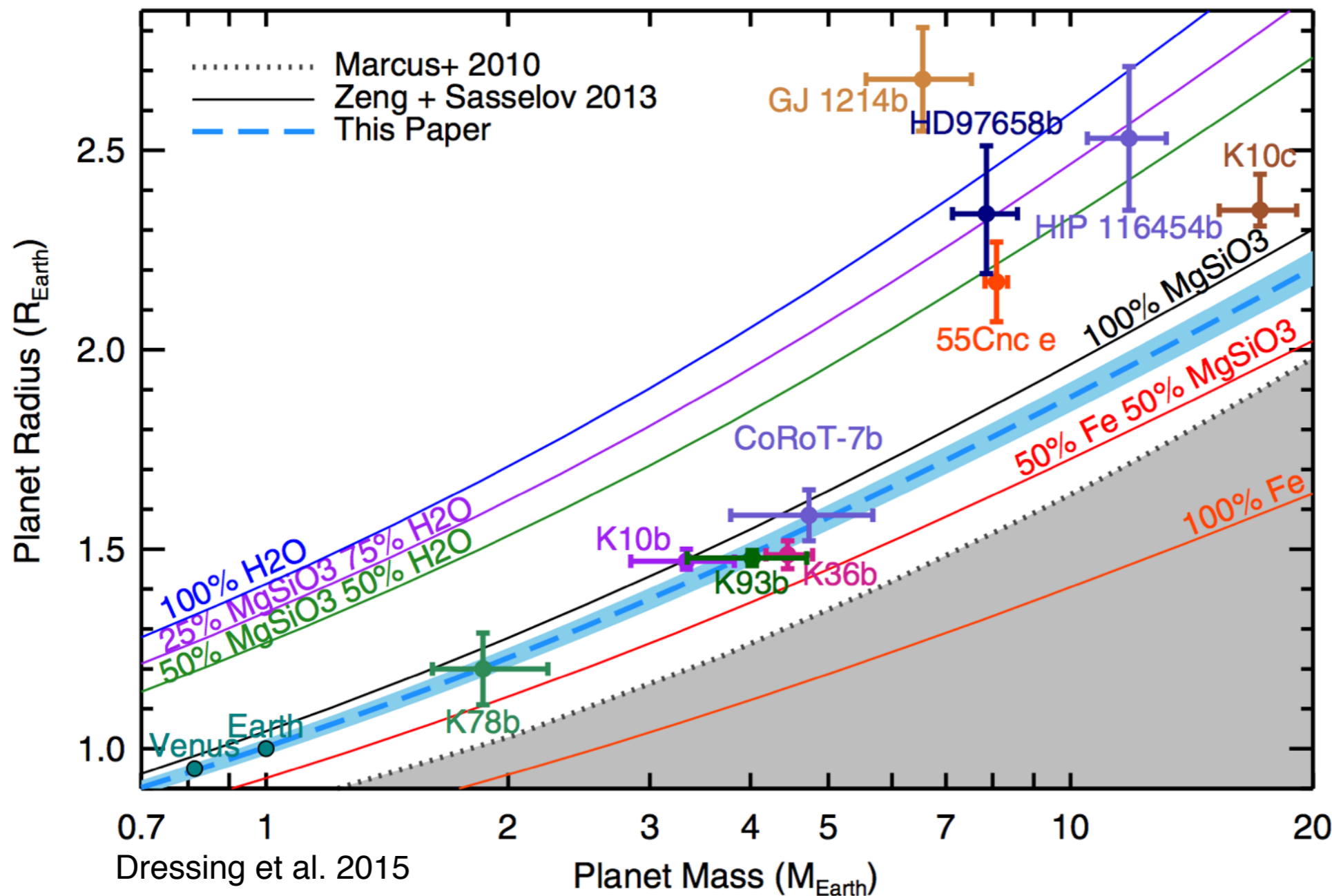




# Iron mass fraction ?

Earth, Mars, Venus (but not Mercury & the Moon):  
~1/3 Iron core : ~2/3 Si mantle (by mass)

*Same as expected from solar composition*



Marboeuf et al. 2014

Dorn et al. 2015

Need stellar chemical composition [Si/Fe], [Mg/Fe]

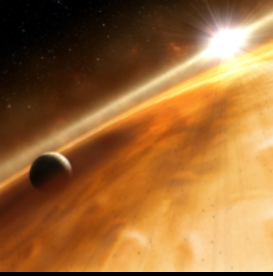
*If H/He excluded (in bare core triangle), and assuming  $f_{\text{iron}}=1/3$  is universal, we can calculate the ice mass fraction from M and R*



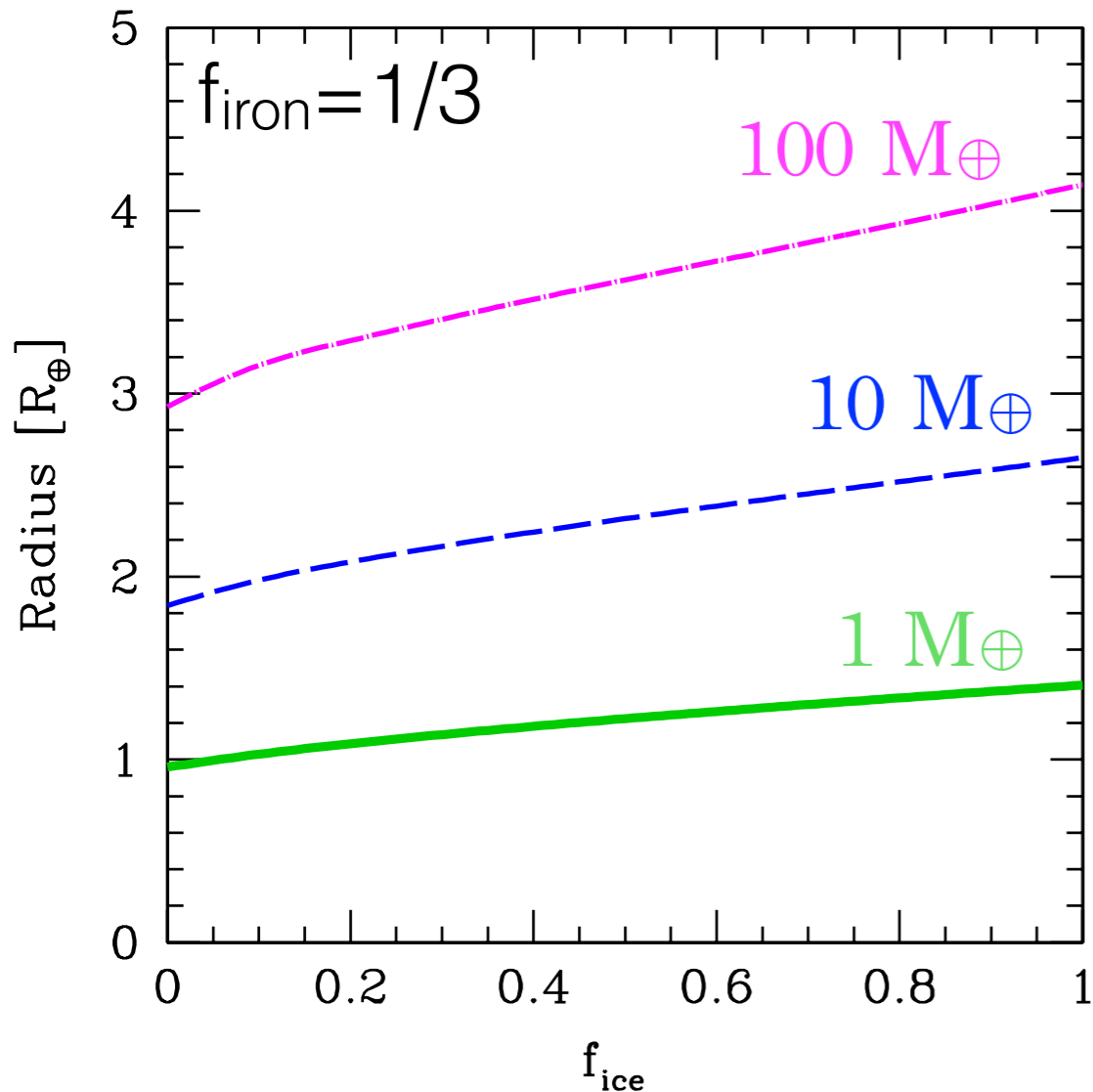
# Fe mass fraction

mass %	Corot-7	Kepler-93	Kepler-10	Sun	Sun (L03)
H	74.83	75.09	74.77	75.06	74.91
He	23.61	23.69	23.61	23.68	23.77
H	0.80	0.55	0.90	0.50	0.51
CH	0.32	0.37	0.36	0.37	0.29
Fe	0.13	0.09	0.09	0.12	(0.17)
MgSiO	0.30	0.07	0.16	0.25	(0.27)
Mg	0	0.14	0.09	0.03	
SiO	0.005	0	0	0	
Z	1.56	1.21	1.61	1.26	1.32
f	29.4	29.1	25.6	31.0	38.0
f	70.6	70.9	74.3	69.0	62.0

32.6%



# Inferring the ice mass fraction



Planets in bare core triangle

- ▶ no H/He
- ▶ assume fixed Earth-like Fe:Silicate fraction for *all* planets ( $f_{\text{iron}} = 1/3$ )

=> can invert

$$M, R \Rightarrow \rho_{\text{nom}} \Rightarrow f_{\text{ice,nom}}$$

*preliminary simplistic analysis:*

*Future work*

*-use actual stellar composition*

*-better treatment of errors*

*-several interior, EOS & evap. models*

## Errors in M and R

$$M + \sigma_M, R - \sigma_R \Rightarrow \rho_{\text{max}} \Rightarrow f_{\text{ice,min}}$$

$$M - \sigma_M, R + \sigma_R \Rightarrow \rho_{\text{min}} \Rightarrow f_{\text{ice,max}}$$

ice presence only constrained if  $f_{\text{icemin}} > 0$





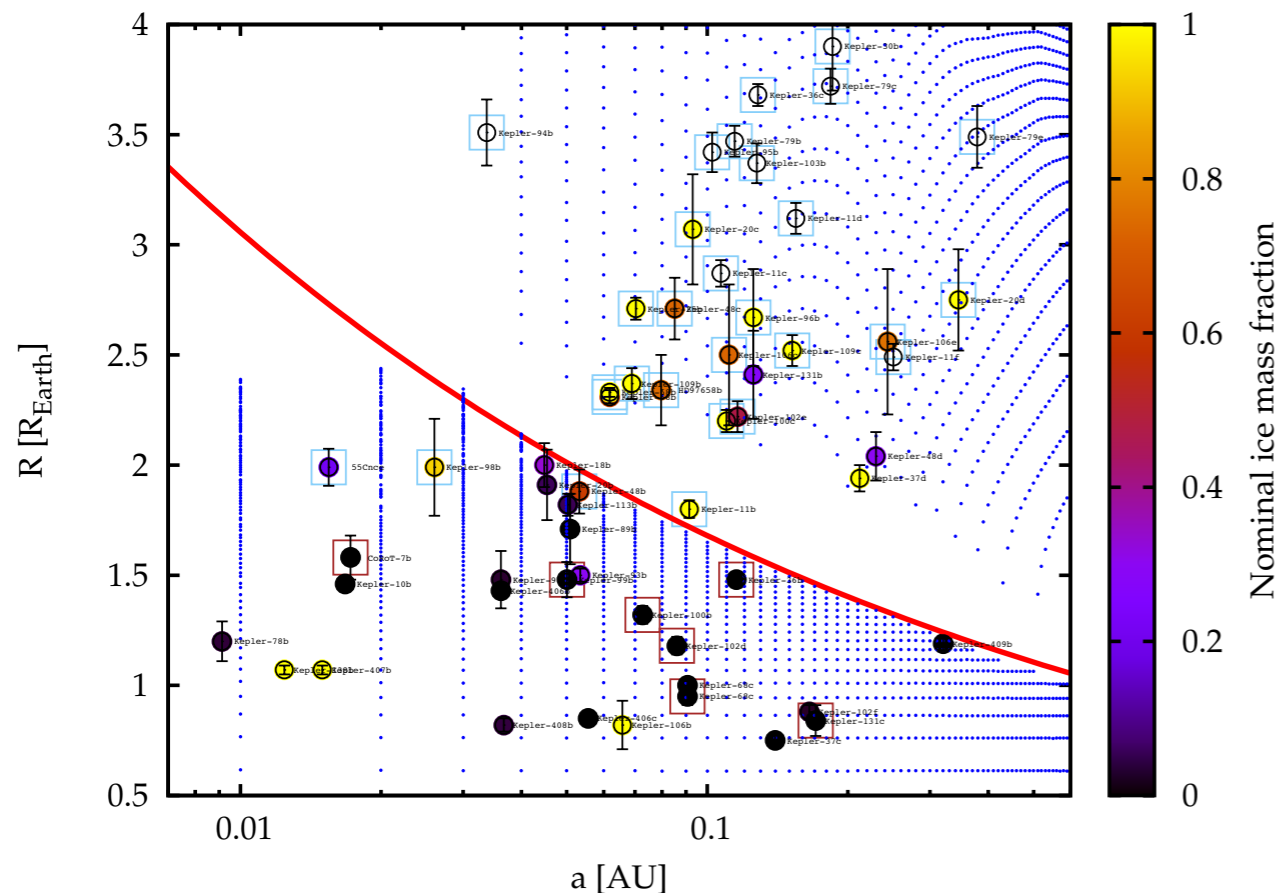
# The ice mass fraction, revealed (?)

	M	R	$f_{ice}$
55 Canc e	$8.3 \pm 0.4$	$1.99 \pm 0.07$	0.03 - 0.20, - 0.34
K-98 b	$3.6 \pm 1.6$	$1.99 \pm 0.22$	0.23- 0.94 - $\geq 1$
K-48 b	$3.9 \pm 2.1$	$1.88 \pm 0.10$	0.11-0.62 $\rightarrow \geq 1$

Orbital migration

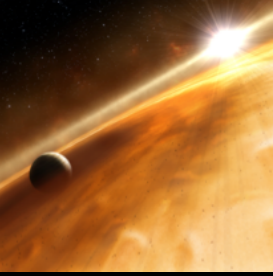
Atmospheric spectra!

55 Canc e: Demory et al. 2011: 20% ice, but see Demory et al. 2015, Madhusudhan et al. 2012, Alibert submitted

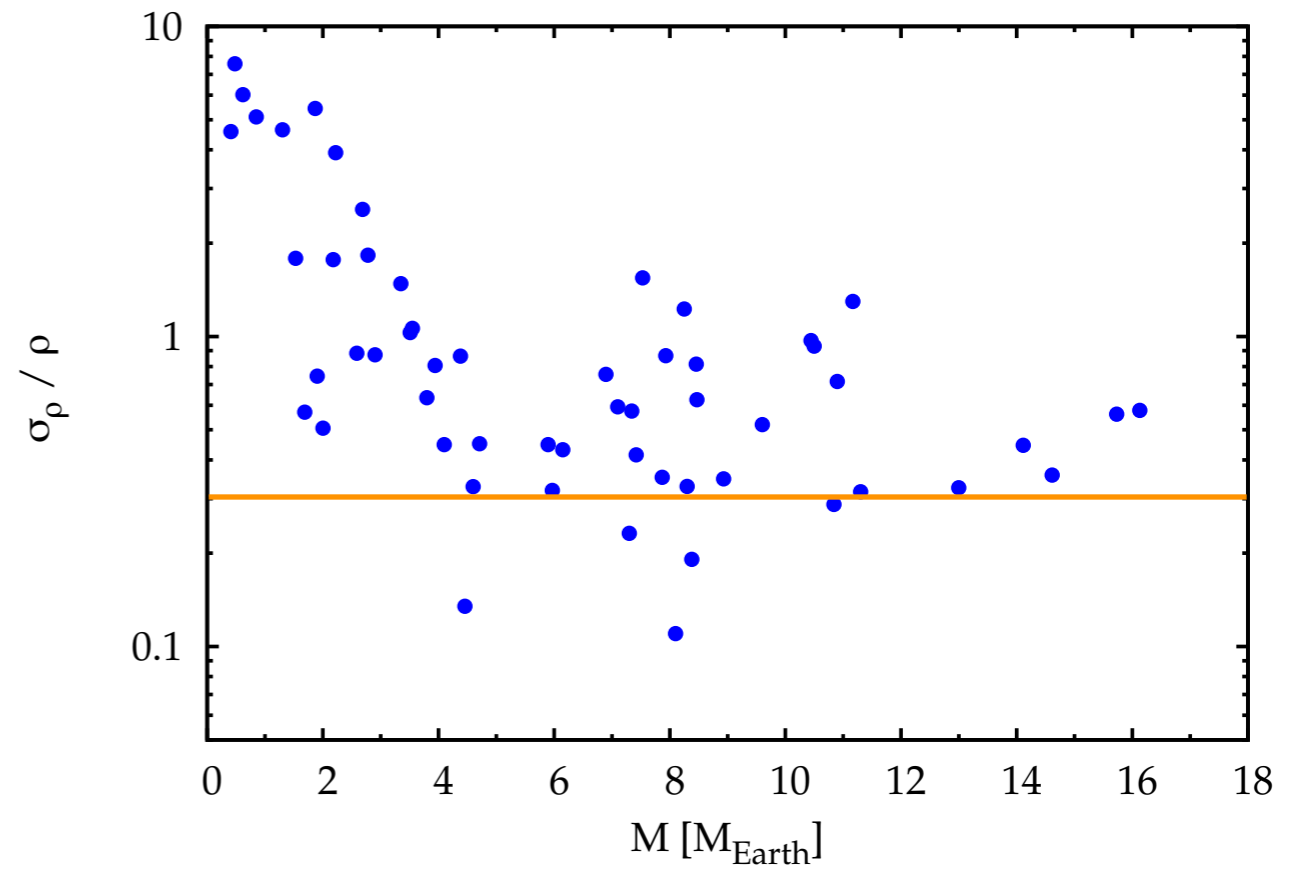
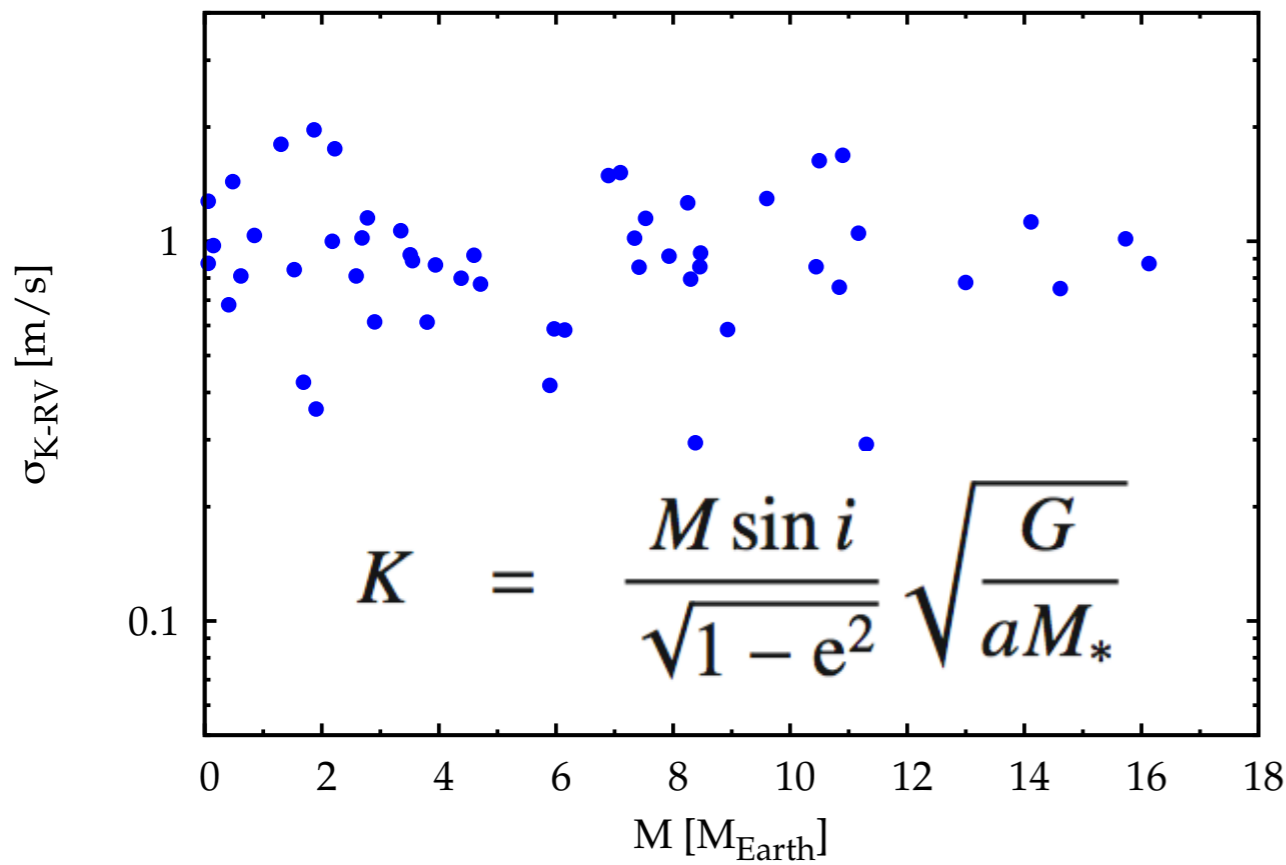
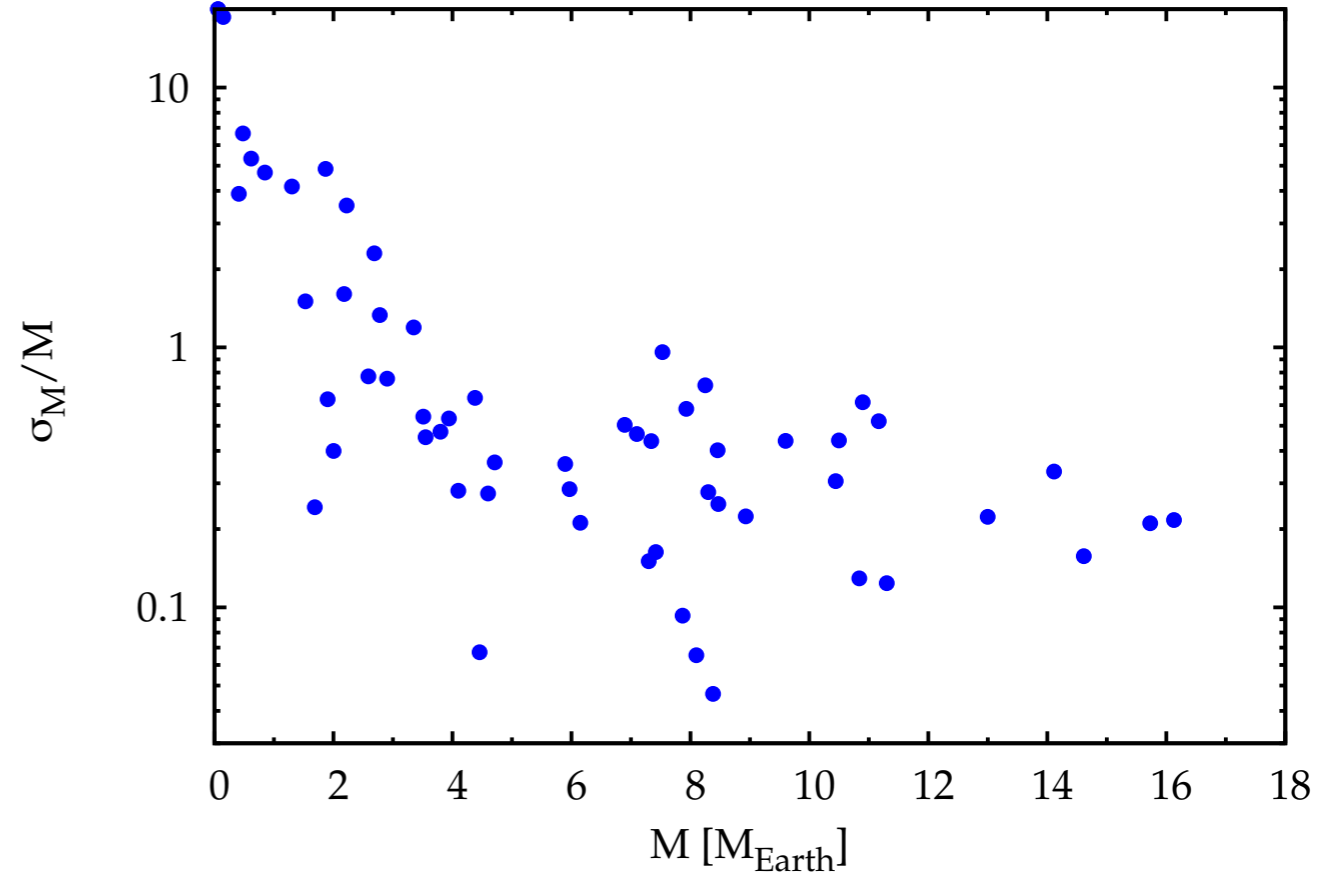
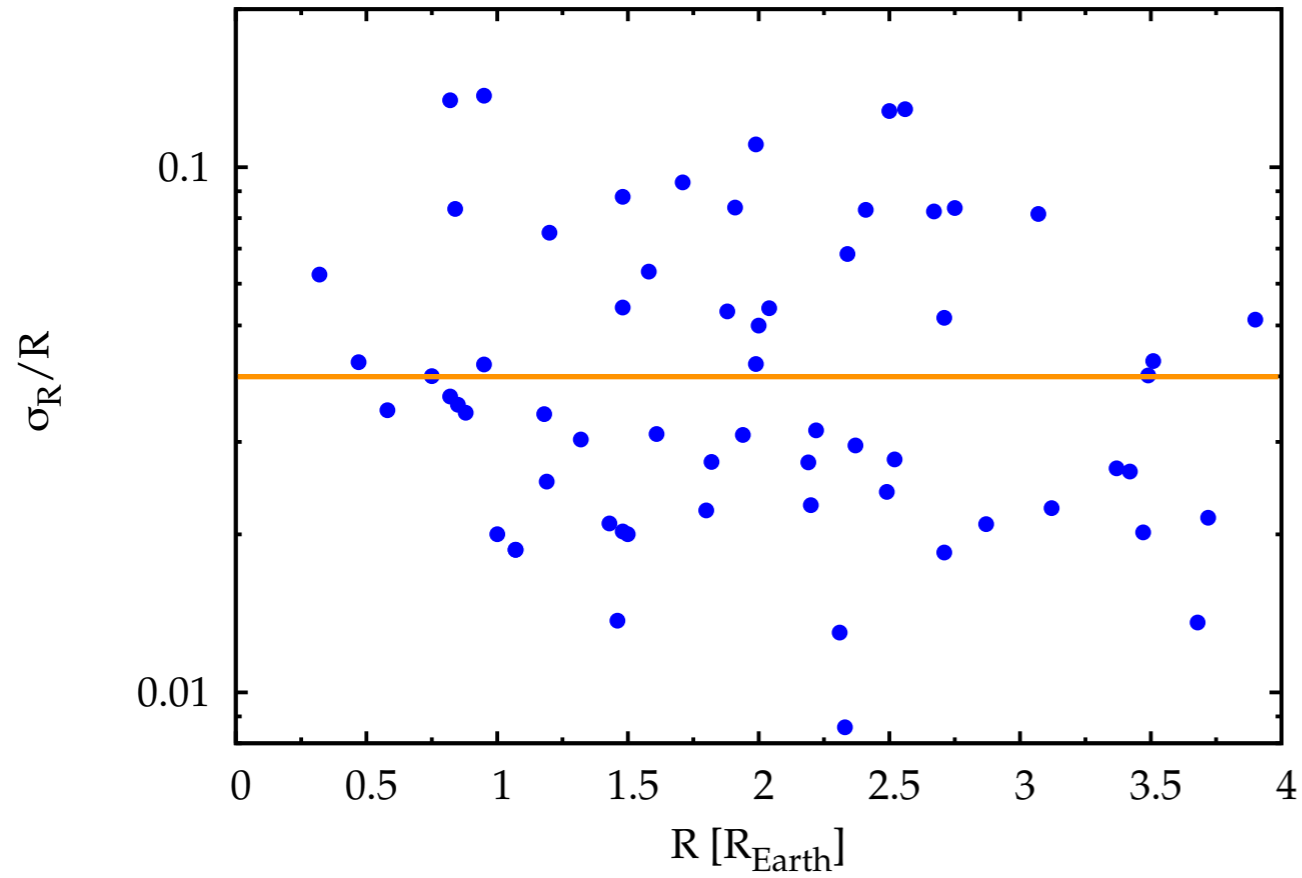


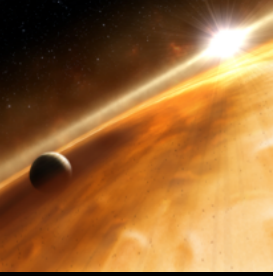
**Statistics:** 57 planets (solar-like host,  $M > 0$ )

- a) 29 outside bare core triangle
  - 3 unconstrained
  - 0 constrained rocky
  - 11 constrained with H/He
  - 15 constrained with H/He or ice
- b) 28 in the bare core triangle
  - 18 unconstrained
  - 7 constrained rocky
  - 3 constrained with ice (but...)



# Impact of M and R errors





# Reducing the errors

**Statistics:** 57 planets (solar-like host,  $M > 0$ )

- a) 29 outside bare core triangle
  - 3 unconstrained
  - 0 constrained rocky
  - 11 constrained with H/He
  - 15 constrained with H/He or ice
- b) 28 in the bare core triangle
  - 18 unconstrained
  - 7 constrained rocky
  - 3 constrained with ice (but...)

Effect of reducing error in radial velocity measurement  $\sigma_{K-RV}$  [m/s]

	WM14	0.6 m/s	0.3 m/s	0.1 m/s
unconstrained outside	3	2	1	0
unconstrained inside	18	14	9	7

# Conclusions

- Ice mass fraction of close-in low-mass planets: key constraint
- M-R degeneracy reduced by taking into account
  - temporal dimension
  - orbital distance
  - chemical composition of host star } atmospheric escape
- Simple analytical models for
  - transition gaseous-solid planet:  $M_{\text{bare}} / R_{\text{bare}}$ 
    - All start with primordial H/He. No outgassing.
  - link stellar photospheric composition - planetary iron mass fraction
    - Earth like values expected for Corot-7b, Kepler-10b, Kepler-93b
- Simplistic analysis of bulk composition of WM14 sample
  - 3 planets might have massive ice shells: orbital migration. But...
  - Much more refined analysis necessary
- Useful for analysis of input of M and R errors: low  $\sigma_{\text{K-RV}} < 1$  m/s needed