L183 (L134N) revisited

III. The gas depletion

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Abstract. We present a detailed study of the gas depletion in L183 (L134N) for a set of important species, namely, CO, CS, SO, N₂H⁺ and NH₃. We show that all these species are depleted at some level. This level seems to depend mostly on a density threshold rather than on dust opacity. Therefore UV shielding would not be a main factor in the triggering of depletion. Our data suggest that CO, CS and SO depletion happen at densities of ∼3 x 10⁴ cm⁻³, while N₂H⁺ and NH₃ seem to deplete at densities close to 10⁶ cm⁻³. The latter result is consistent with the Bergin & Langer (1997, ApJ, 486, 316) polar (H₂O) ice case but not with the more recent models of Aikawa et al. (2003, ApJ, 593, 906). CS depletion occurs much below its (J;2–1) critical density, (7 x 10⁵ cm⁻³) and therefore makes this species unsuitable to study the density structure of many dark cloud cores.

Key words. ISM: abundances – ISM: molecules – ISM: dust, extinction – ISM: individual: objects: L183 (L134N) – radio lines: ISM

1. Introduction

In the very cold, shielded interior of dark molecular clouds, most molecules except H-only species and possibly N-carriers are expected to stick to grains and thus disappear from the gas phase. This has been anticipated as early as a few years after the discovery of CO. Because CO was predicted to deplete onto grains at temperatures below 20 K, it was not clear why it could still be seen in 10 K clouds. Yet, no clear trace of depletion could be found for any species until facilities for observing and measuring cold dust became available. In the mid-nineties, bolometer arrays (MAMBO at 1.2 mm, SCUBA at 850 and 450 µm) have allowed astronomers to detect dense cold dust cores which had escaped all searches so far because C¹⁸O, which was supposed to trace gas column-density in cold molecular clouds and thus locate cores via their high mass content, was in fact depleted inside these quiescent cores. Cores were thus found from dust emission eventually and more recently via near or mid infrared dust absorption. As a direct consequence, CO (and other molecules) depletion was eventually revealed. While depletion itself is no longer questioned, the physical conditions it requires for different species are not yet well-established. Polar molecules such as H₂O freeze onto grains at temperatures below ∼100 K and apolar molecules (like CO) below ∼20 K, but N-bearing species, such as NH₃ and N₂H⁺ do not seem to experience this as they are seen deep inside the cores and could even act as surrogate dust tracers. It is thus necessary to track depletion in as many cold clouds as possible to shed light on the details of the depletion mechanism. A second reason to study depletion is linked to astrochemistry. Without taking depletion effects into account, all species are considered to be spatially coexistent when they are not (N₂H⁺ cannot coexist with CO e.g., Bergin & Langer 1997; Caselli 2002) and therefore relative abundances are not correctly evaluated. This is one of the reasons why previous abundance estimates made towards L183 by Swade (1989b) and by Dickens et al. (2000) should be considered very cautiously before checking astrochemical models against them. We have therefore undertaken to revisit this source in order to establish it as a true reference for chemical models.

Depletion was revealed in L183 for the first time by Pagani et al. (2002, hereafter Paper I) and independently confirmed by Juvela et al. (2002). However, in both works the depletion estimates were done by comparison with the ISOPHOT 100 and 200 µm data which only probe a thin outer layer (0–15 AV) of cold (12–17 K) dust. Therefore the depletion along the

* Based on observations made with the CFHT, the Iram 30-m and the ARO 12-m (formerly NRAO 12-m).
** Appendix A is only available in electronic form at http://www.edpsciences.org
line-of-sight was evaluated to a factor of 1.5–2 only. As we showed in a subsequent paper (Pagani et al. 2004, hereafter Paper II), these early estimates are not correct because they ignore the bulk of the dust, which is at $T < 10$ K and does not emit at 200 $\mu$m. Therefore, depletion has been strongly underevaluated in these earlier works. We have now obtained (Paper II) a composite Mid- and Near-Infrared dust absorption map which traces all the dust column density, together with a map of the dust emission at 1.2 mm, and therefore we can work out more precisely the depletion effects in this source.

In this paper, we will present in Sect. 2 the molecular line observations we have made, analyze them in Sect. 3 and discuss the depletion effects we find by comparison with our dust map from Paper II in Sect. 4. In Sect. 5, we will draw our conclusions.

2. Observations

We have observed four species, namely CO, CS, SO and N$_2$H$^+$, and for each species at least two isotopomers and for each isotopomer at least 2 transitions (except for the N$_2$H$^+$ isotopomer for which we have only a few J=2–3 observations with low signal-to-noise ratio). For the goals of the present work, we concentrate on a small subset of these observations (Table 1) complemented with observations from Tiné et al. (2000). The remaining observations will be published in subsequent papers. The reference position of the source in this study is: 15$^h$54$^m$06.6$^s$, $-2^\circ$52$'$19\" (J2000) which is the L134N reference position given by e.g. Swade (1989a) and the LSR velocity is $+2.5$ km s$^{-1}$. Note however that the SIMBAD position for this source is 15$^h$54$^m$09.2$^s$, $-2^\circ$51$'$39\" (J2000) and that a few other reference positions are also found in the literature. We would suggest using the central position of the dust peak from now on as the reference in further work: 15$^h$54$^m$06.6$^s$, $-2^\circ$52$'$43\" (J2000).

The subset of observations presented here have been carried out with either the Kitt Peak 12-m (formerly owned by NRAO, now operated by the University of Arizona, hereafter KP 12-m) or the IRAM 30-m.

2.1. Kitt Peak 12-m data

Observations started in December 1999 at Kitt Peak and spanned a seven month period. Complementary observations were obtained in January 2001. The Kitt Peak 12-m is equipped with two-polarization receivers at 1.3, 2 and 3 mm with filter banks and a versatile autocorrelator in parallel as backends. We used 100 kHz filters all the time and the 32K-channel ter banks and a versatile autocorrelator in parallel as backends. We would suggest using the central position of the dust peak as the reference in further work: 15$^h$54$^m$08.5$^s$, $-2^\circ$52$'$43\" (J2000).

IRAM 30-m data

IRAM 30-m data were collected in April, May, December 2003 and May 2004. The IRAM 30-m is equipped with two polarization receivers at 1.1, 1.3, 2 and 3 mm. It has filter banks and a versatile autocorrelator. The system allows to observe up to 4 different lines simultaneously. We worked with a frequency resolution of 20 kHz at 2 and 3 mm, giving us a velocity resolution around 50 m s$^{-1}$ at 3 mm and 35 m s$^{-1}$ at 2 mm. At 1.3 mm, we worked with 40 kHz resolution to keep the same 50 m s$^{-1}$ velocity resolution. Pointing and focus were checked every 90 min on close-by continuum sources. The observations have been performed in frequency switch mode. We observed a few positions in N$_2$H$^+$ and N$_2$D$^+$ in April and May 2003.

Table 1. Observational parameters and sensitivity.

<table>
<thead>
<tr>
<th>Molecule</th>
<th>Transition</th>
<th>Frequency (MHz)</th>
<th>Beam size (arcsec)</th>
<th>rms$^a$ (K)</th>
</tr>
</thead>
<tbody>
<tr>
<td>C$^{18}$O</td>
<td>J=1–0</td>
<td>109 782.163</td>
<td>57$_{KP}$</td>
<td>0.11</td>
</tr>
<tr>
<td>C$^{18}$O$^b$</td>
<td>J=1–0</td>
<td>109 782.163</td>
<td>23$_{I}$</td>
<td>0.059</td>
</tr>
<tr>
<td>C$_2$H$_4$</td>
<td>J=2–1</td>
<td>219 560.327</td>
<td>28$_{KP}$</td>
<td>0.26$^c$</td>
</tr>
<tr>
<td>C$_2$H$_4$</td>
<td>J=2–1</td>
<td>219 560.327</td>
<td>12$_{I}$</td>
<td>0.12$^c$</td>
</tr>
<tr>
<td>C$_2$H$_4$</td>
<td>J=1–0</td>
<td>112 359.277</td>
<td>56$_{KP}$</td>
<td>0.034</td>
</tr>
<tr>
<td>C$_2$H$_4$</td>
<td>J=2–1</td>
<td>97 980.950$^a$</td>
<td>64$_{KP}$</td>
<td>0.088</td>
</tr>
<tr>
<td>32SO</td>
<td>J$_2$:2–3</td>
<td>99 299.879</td>
<td>63$_{KP}$</td>
<td>0.12</td>
</tr>
<tr>
<td>N$_2$H$^+$</td>
<td>J=1–0</td>
<td>93 173.384$^d$</td>
<td>67$_{KP}$</td>
<td>0.14</td>
</tr>
<tr>
<td>N$_2$H$^+$</td>
<td>J=1–0</td>
<td>93 173.384$^d$</td>
<td>27$_{I}$</td>
<td>0.037</td>
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<tr>
<td>N$_2$D$^+$</td>
<td>J=2–1</td>
<td>154 217.096$^d$</td>
<td>16$_{I}$</td>
<td>0.050</td>
</tr>
<tr>
<td>N$_2$D$^+$</td>
<td>J=3–2</td>
<td>231 321.757$^d$</td>
<td>12$_{I}$</td>
<td>0.097</td>
</tr>
<tr>
<td>NH$<em>2$D$</em>{para}$</td>
<td>J$_{K+1}$:1$^a(11–10)$</td>
<td>110 153.587$^e$</td>
<td>23$_{I}$</td>
<td>0.054</td>
</tr>
</tbody>
</table>

$^a$ Median value over the map.

$^b$ Data partly from Tiné et al. (2000).

$^c$ Frequency is taken from Pagani et al. (2001).

$^d$ Hyperfine components.

$^e$ Small map towards Peak E only.

$^f$ IRAM 30-m telescope.

KP NRAO/ARO KP 12-m.
Fig. 1. Comparison of $^{13}$CO ($J:1–0$) (left) and ($J:2–1$) (right) spectra (towards peak E) from the Kitt Peak (KP) 12-m and IRAM 30-m telescopes after smoothing the latter to the KP 12-m resolution (1′ for the ($J:1–0$) and 30″ for the ($J:2–1$) transitions). Coordinates are offsets in arcmin from reference position. X axis (velocity) scale is from 0 to 5 km s$^{-1}$, and Y axis ($T_\ast$) scale is from −0.5 to 4.0 K ($J:1–0$) and from −0.3 to 2.2 K ($J:2–1$).

$T_{\text{sys}}$(SSB) were 100 K at 3 mm, 300 K at 2 mm and 400 to 700 K at 1.3 mm. The reader is referred to Tiné et al. (2000) for the description of their observations. We performed further observations of the N$_2$D$^+$ ($J:2–1$) line in December 2003 to improve and enlarge Tiné’s map to a size of 100′′ × 200′′. We also mapped the N$_2$D$^+$ ($J:3–2$) transition. For both transitions, $T_{\text{sys}}$ were similar to what we obtained in Spring 2003. The 1.3 mm receiver we used was HERA (9 pixels spaced by 24′′) with the new autocorrelator, VESPA. We observed the N$_2$D$^+$ ($J:2–1$) line with 10 kHz resolution (=20 m s$^{-1}$) and the N$_2$D$^+$ ($J:3–2$) line with 40 kHz resolution (=50 m s$^{-1}$).

2.3. Calibration

The KP 12-m telescope forward scattering and spillover efficiency ($\eta_{\text{fss}}$, Kutner & Ulrich 1981) has been measured to be 0.64 at all wavelengths. This efficiency allows to calibrate our data in the $T_\ast$ scale if we suppose the beam coupling to the source to be 1. Though the exact definition of the $T_\ast$ scale depends on what angular size we use to measure $\eta_{\text{fss}}$, its general acceptance (or its closest approximation, $\eta_{\text{moon}}$) applies to calibrate signals from extended sources larger than the main beam, such as L183 (see Teyssier et al. 2002, for a recent discussion on this point). For the IRAM 30-m, the forward efficiency ($\eta_f$) is identical to $\eta_{\text{moon}}$ which means that for extended sources such as L183, it is less erroneous to use $\eta_f$ than to use the main beam efficiency, $\eta_{\text{MB}}$, which introduces too large a correction. In other words, for the IRAM 30-m, $T_\ast \approx T_\ast^f$.

Indeed, we find (Fig. 1) that for $^{13}$CO ($J:1–0$) and ($J:2–1$), the IRAM 30-m telescope gives comparable results to the KP 12-m telescope after convolution at the KP 12-m resolution if we use the IRAM 30-m $T_\ast^f$ scale and the KP 12-m $T_\ast$ scale. This indicates that the calibration of both telescopes is consistent for extended emission tracers. If we had applied the $\eta_{\text{MB}}$ correction for both telescopes then the IRAM 30-m ($J:1–0$) line would have been 23% stronger than the KP 12-m line while the KP 12-m ($J:2–1$) line would have been 26% stronger than the IRAM 30-m line, which would have lead to considerable discrepancies in the ($J:2–1$)/($J:1–0$) line ratios.

3. Results

Because of its importance in this work, we redisplay first the dust map (Fig. 2) we obtained in Paper II with arrows marking
Fig. 3. \(^{18}\)O \((J:1–0)\) integrated intensity contours (from the KP 12-m telescope) superimposed on the dust map from Paper II (in log grey scale). Coordinates are J2000 equatorial. \(^{18}\)O levels: 0.2 to 1.8 by 0.2 K km s\(^{-1}\) (rms \(\approx\) 35 mK km s\(^{-1}\)). The white and black dashed contour represents the \(A_V = 20\) mag level. Letters C, E, N, S, and W mark the molecular peaks (see text) and the KP 12-m beam size is displayed in the top right corner.

Fig. 4. Same as Fig. 3 for \(^{17}\)O \((J:1–0)\). \(^{17}\)O levels: 0.1 to 0.7 by 0.1 K km s\(^{-1}\) (rms \(\approx\) 30 mK km s\(^{-1}\)).

Fig. 5. Same as Fig. 3 for \(^{32}\)S \((J:2–1)\). \(^{32}\)S levels: 0.1 to 1.1 by 0.2 K km s\(^{-1}\) (rms \(\approx\) 45 mK km s\(^{-1}\)).

Fig. 6. Same as Fig. 3 for \(^{32}\)SO \((J:3–2)\). \(^{32}\)SO levels: 0.3 to 2.1 by 0.3 K km s\(^{-1}\) (rms \(\approx\) 60 mK km s\(^{-1}\)).

Both the places of the molecular peaks (C, N, S and W) described by Dickens et al. (2000) to which we have added a fifth molecular peak, E (see below), and the places of the nearby dust peaks which we have numbered from 1 to 5.

3.1. Large-scale Kitt Peak maps

Figures 3–7 show \(^{18}\)O, \(^{17}\)O, \(^{32}\)S, \(^{32}\)SO, and \(N_2H^+\) emission intensity superposed as contours on the dust map image from Paper II (see Fig. 2). For the dust map, the \(A_V = 20\) mag contour is emphasized.

For both \(^{18}\)O (Fig. 3) and \(^{17}\)O (Fig. 4) \((J:1–0)\) lines, it is clear that none of the four molecular peaks (N, S, C, W) described by Dickens et al. (2000) is visible (except a very small \(^{18}\)O peak towards Peak C but with no counterpart in \(^{17}\)O). To the east, there is a \(^{18}\)O/\(^{17}\)O peak which coincides with our dust peak # 5 (Fig. 2 and Paper II) and which we label E to keep consistency with Dickens et al. (2000, this peak is outside their \(^{18}\)O map). Interestingly enough, this dust peak # 5 reaches an optical extinction of \(A_V \approx 25\) mag. While \(^{18}\)O does show opacity effects (as mentioned in Paper I), it is not the case for \(^{17}\)O (the main hyperfine component is approximately ten times weaker that the \(^{18}\)O line). Both isotopomers show the same features and thus the absence of the four N, S, C and W peaks is not due to opacity effects but is real.

The \(^{32}\)S \((J:2–1)\) line emission map (Fig. 5) shows no correlation with any of the five peaks but only a general increase towards the center of the cloud. However, the emission...
peak is situated north-west of peak W, noticeably outside of the
dust cloud core and the line is obviously optically thick as its
self-reversed profile indicates\(^1\) and the question of peak hiding
in the map arises again.

The \(^{32}\)SO (J\(^{1}\)=3\(^2\)–2\(^1\)) line emission map (Fig. 6) shows a
good correlation with two of the peaks (W and S) with a small
extension towards peak C. It does not extend as far to the north
as the CO and CS lines but is otherwise as extended as \(^{13}\)CO. However, the strongest SO peak is the W peak and not the
C peak while the dust content is 4 times as high towards dust
peak 1 than towards dust peak 3 (see Fig. 2).

Finally, the \(N_{2}H^+\) (J\(^{1}\)=1\(^0\)–0\(^0\)) map (Fig. 7) is clearly different
from the previous four as its extent is much more limited. It is
rather well correlated with the dust content above \(A_V\approx 20\) mag
with two prominent peaks coincident with molecular peaks N
and C and two extensions reaching peaks W and S. Peak E is
conspicuously absent (a very weak line, 0.15 K peak intensity –
a 4\(\sigma\) detection – has been detected though). It is remarkable
then that the only \(^{18}\)O/\(^{17}\)O peak coinciding with a dust peak
is the only peak which hardly emits in \(N_{2}H^+\) (J\(^{1}\)=1\(^0\)–0\(^0\)). Overall,
CO and \(N_{2}H^+\) maps are completely unrelated.

While all these differing features could have looked puzzling fifteen years ago when looking at Swade’s maps (Swade 1989a),
we now know that the main reason behind these differences is
the depletion of CO, CS and SO onto grains, as we will
discuss below. Tafalla et al. (2002) recently reached the same
conclusions towards other pre-stellar cores.

3.2. Small scale maps and cut

These maps concern data taken with the IRAM 30-m telescope
with resolutions in the range 11–23\(\arcsec\).

Tiné et al. (2000) mapped a small region around the
central molecular peak (peak C) with the IRAM 30-m

\(^1\) Dickens et al. (2000) advocated the existence of two independent
peaks instead of a self-absorption feature, due to the use of an ero-
neneous CS frequency, see Pagani et al. (2001).

4. Depletion effects

Two difficulties arise in the search for depletion effects. The
first one is to have a correct estimate of the dust content. For
example, Willacy et al. (1998) have used ISOPHOT 100 and
200 \(\mu\)m data to estimate the dust content in the very cold source
L1498. While the \(^{13}\)CO depletion is unquestionable in that
source, the dust is probably largely underestimated (as noted
by the authors themselves) because the 200 \(\mu\)m emission does
not trace dust below 10 K as we also show in Paper II. As men-
tioned above, we (Paper I) and Juvela et al. (2002) met the
same problem. The second difficulty is to have a correct estimate of
the species column density. For example, in cold clouds, with
high gas column densities, \(^{13}\)CO can become optically thick.
In fact, if it were not for depletion effects, optically thick \(^{13}\)CO
would be very wide-spread in dark clouds with optical extinc-
tion above \(A_V\approx 20\) mag. One solution is to use \(^{17}\)O instead
but the line is weak and difficult to map on large areas. Another
solution is to map the \(^{18}\)O (J\(^{2}\)=2\(^0\)–1\(^0\)) and (J\(^{3}\)=3\(^0\)–2\(^0\)) transitions and
run detailed radiative transfer models. It is a time-consuming
task too and the result is not straightforward as it implies some
interpretation of the data prior to diagnosing depletion effects.
The question thus often arises to know whether the \(^{18}\)O intensity
flattening commonly observed towards the cores of cold
dark clouds is really due to depletion or instead to radiative
transfer effects such as optically thick gas or extremely cold
(5–6 K) gas which could induce the same behaviour. Tafalla
et al. (2002) have shown that depletion is the only possible ex-
planation for the five starless cores they have studied and most
published cases usually show equivalent \(^{17}\)O behavior which
rules out opacity effects. Low temperatures are usually thought
difficult to justify from NH\(_3\) and CO measurements. Here we
are going to discuss depletion effects for CO, CS and SO on the

\(^2\) The low resolution of Dickens et al. (2000) data probably explain
that their peaks seems slightly displaced eastward.
large scale and then the depletion effects we see with nitrogen-bearing species (N$_2$H$^+$, N$_2$D$^+$, and NH$_2$D).

4.1. CO depletion

If we plot the pixel-to-pixel comparison of the C$^{18}$O integrated intensity versus the dust optical extinction and combine the two sets of C$^{18}$O data (KP 12-m and IRAM 30-m), we obtain the very clear-cut picture of depletion of Fig. 10. The $A_V$ data (Paper II) have been smoothed to each telescope resolution and thus the peak opacity is only ~100 mag now for a 23$''$ beam and ~50 mag for a 60$''$ beam. The turn-over is abrupt and occurs at $A_V$ ~ 20 mag. This is a factor of 2–3 higher than the value found by Bergin et al. (2002) in B68 where C$^{18}$O saturation starts at $A_V$ ~ 7 mag and becomes flat at $A_V$ ~ 10 mag, or by Kramer et al. (1999) in IC 5146 and by Alves et al. (1999) in L977 where depletion is found to start at $A_V$ ~ 10 mag for both sources. Thus except for peak E (or dust peak 5) all the region inside the $A_V$ = 20 mag contour is depleted of CO isotopeomers. The C$^{18}$O depletion surface covers ~25$^2$, a wide area indeed which explains the poor resemblance between the C$^{18}$O map and maps of several other species in this source. A possible marginal increase of the C$^{18}$O integrated intensity is still visible beyond the depletion turnover. A linear fit is not physical because the depletion probably increases going deeper into the core but the slope gives a good lower limit to the depletion we observe here. We have fitted the Kitt Peak data for $A_V$ < 20 mag on the one hand and the whole IRAM data on the other hand (Fig. 10). We find a slope of 87 and 2.0 mK km s$^{-1}$ mag$^{-1}$ respectively. The decline in abundance from the region below to the region above $A_V$ ~ 20 mag is thus larger than ~43 on average (and the line of sight depletion is about 5 for the peak opacity). Below $A_V$ ~ 20 mag, the C$^{18}$O abundance is ~1.1 $\times$ 10$^{-7}$, though the detailed Monte-Carlo analysis performed for two positions (Paper I) and which yields higher column densities than the simpler LVG analysis indicates a C$^{18}$O abundance close to 1.4 $\times$ 10$^{-7}$, quite comparable to the value given by Frerking et al. (1982).

As discussed in Sect. 3, the comparison between C$^{18}$O and C$^{17}$O maps shows identical features between the two isotopomers and thus the opacity of the C$^{18}$O ($J=1$–0) is relatively small and cannot explain the absence of molecular peaks towards the main dust peak. Low temperatures are not a better explanation since, on the one hand, 40$''$ away from the dust peak, i.e. towards the L134N reference position, we have estimated the C$^{18}$O total column density to be 2.7 $\times$ 10$^{15}$ cm$^{-2}$ (Paper I) and, on the other hand, the line intensities of the C$^{18}$O transitions change very little between the two positions, and therefore the C$^{18}$O column density should be approximately the same towards the dust peak. From the dust peak estimated $A_V$ (~100 mag for 23$''$ resolution) and using $X$(C$^{18}$O) = 1.4 $\times$ 10$^{-7}$, we would have expected a total C$^{18}$O column density of ~1.4 $\times$ 10$^{16}$ cm$^{-2}$ in that direction if there were no depletion. A mean temperature of ~6 K along the line of sight would be compatible with the observations but is unrealistic taking into account the envelope higher temperature (10–12 K). We would be forced to put the core close to 3 K to prevent excess C$^{18}$O emission. On top of that, the ($J=1$–0) line opacity would be ~10, which is not compatible with the C$^{18}$O measurements. We would also have obtained 1.7 K for the main C$^{17}$O component instead of the observed 0.4 K. Depletion is indeed the best explanation we presently know of.

4.2. CS depletion

Contrarily to C$^{18}$O, the CS line is optically thick almost everywhere and the question is whether the opacity hides the dust peaks or if depletion prevents CS from revealing them. In fact, opacity is not the good reason: as Penzias (1975) has shown (see also Linke et al. 1977), if a line is optically thick
Fig. 9. North-south cut through the dust peak (RA offset = +30′′). The histogram displays the 1.2 mm dust emission while the sets of dots trace N-bearing species through the peak. The vertical scales are all arbitrary. They are set to have the species integrated intensities proportional to the dust emission on the peak sides. Except when specified, all data come from the IRAM 30-m. For NH$_2$D and N$_2$D$^+$ (J:2–1), we have also plotted the sum of all the optically thin hyperfine components (dotted lines and crosses) while for N$_2$H$^+$ (J:1–0), we have plotted the only hyperfine component (($J_{F_1,F_0}$:1–0), dashed line and crosses) which remains optically thin ($\tau \leq 1$) in this cut. Error bars are 1$\sigma$ errors on the integrated intensities.

and subthermally excited, then its intensity is merely proportional to its column density (this is illustrated in Appendix A). However, this is true only for a uniform gas slab. Here, a dilution of the peak emission in the surrounding gas is still to be expected and Penzias’ prediction is only to be considered on a large scale. However, the CS peak emission is noticeably asymmetrical compared to the cloud core (Fig. 5), and a preliminary Monte-Carlo analysis has confirmed that the observed CS emission can be explained with densities lower than the critical density (Paper I). Therefore, we think that despite its optical depth, the C$^{34}$S (J:2–1) map is not hiding the peaks (a limited preliminary optically thin C$^{34}$S (J:2–1) map confirms this point).

Though the CS map (Fig. 5) is somewhat different from the C$^{18}$O map (Fig. 3), apart from their similar extent, their intensities are mostly proportional (Fig. 11). The proportionality factor is 0.48 and the reason is that C$^{18}$O is easier to thermalize than CS. As mentioned above, this is due to the fact that CS (J:2–1) is subthermally excited and optically thick and thus its intensity is proportional to its column density. On the contrary, the C$^{18}$O integrated intensity is also proportional to its column density because the (J:1–0) transition is thermalized and optically thin in most of the considered range. Therefore it is not surprising to find that CS has the same depletion behaviour as C$^{18}$O (Fig. 12). CS depletion has been observed before (see, e.g., Tafalla et al. 2002). A preliminary radiative transfer analysis (Paper I) has shown that the
Fig. 12. $^{32}$S ($J:2\rightarrow1$) integrated intensity (KP 12-m data) cross-correlated with $A_V$ data degraded to 1’ resolution.

Fig. 13. $^{33}$SO ($J:3\rightarrow2$) and C$^{18}$O ($J:1\rightarrow0$) integrated intensity cross-correlation. KP 12-m data only. Square symbols represent the average of the $^{32}$SO values per 0.2 K km s$^{-1}$ C$^{18}$O intervals. Error bars represent the 1σ dispersion. The straight line goes through the origin to the 9th average value, its slope is 0.78.

C$^{35}$S and C$^{34}$S transitions ($J:1\rightarrow0$, $J:2\rightarrow1$ and $J:3\rightarrow2$) towards the L134N reference position can be explained by densities $\leq 3 \times 10^4$ cm$^{-3}$, more than an order of magnitude below the CS ($J:2\rightarrow1$) critical density ($n_c = 7 \times 10^5$ cm$^{-3}$). These findings are consistent and point to the fact that CS cannot be used as a density tracer at all in cold dark clouds because it is depleted much below its critical density. The sudden drop for $\langle I(C^{18}O) \rangle = 1.9$ K km s$^{-1}$ average will be discussed in Sect. 4.4.

4.3. SO depletion

Comparison of SO versus C$^{18}$O (Fig. 13) shows that SO hardly appears below a C$^{18}$O intensity of 0.6 K km s$^{-1}$ (equivalent to $A_V = 5$ mag) and that there is no proportionality above that limit (again, the sudden drop for $\langle I(C^{18}O) \rangle = 1.9$ K km s$^{-1}$ will be discussed in Sect. 4.4). Its emission strength correlates somewhat with the C, W and S peaks (Fig. 14), but is not, or only weakly, correlated with peaks N and E which could mean that it comes closer to the C, W and S peaks than CS. Interestingly enough, Bergin & Langer (1997) find that after about 1 My of evolution, when C and consequently CS have already started to deplete, there is a strong enhancement of SO before it starts depleting too. This enhancement has an amplitude of almost two orders of magnitude and SO eventually becomes more abundant than CS, while the model starts with a CS/SO ratio of $\sim 100$. Aikawa et al. (2003, their Figs. 3 to 5) show a similar SO enhancement in some of their depletion models as a function of core distance, though the effect does not reach the same amplitude; i.e. SO never becomes more abundant than CS but the increase of its column density as a function of radial proximity to the core center is clearly visible. We have some hints of this effect here but we can only do a preliminary analysis for the following reason: there are no SO collision coefficients yet at low temperatures (<50 K, Green 1994) to make a non-LTE analysis of its excitation and thus only a rotational diagram analysis is presently possible. However, due to opacity effects, as explained by Goldsmith & Langer (1999), and to low excitation temperature, this analysis is difficult to perform and requires many lines. We have shown that without proper corrections, SO column density would be underestimated by 2 orders of magnitude using such a diagram (Paper I). Though we presently lack data to study in detail the CS/SO column density ratio in L183, we have evaluated the CS and SO column densities towards the reference position (Paper I) for which we have observed many SO transitions and could gather a few more data from the literature. We have found $N(CS) = 1.4 \times 10^{13}$ cm$^{-2}$ and $N(SO) = 2.5 \times 10^{13}$ cm$^{-2}$, or a CS/SO ratio $\approx 0.056$. In addition, CS is more extended than SO (Figs. 5 and 6) implying that away from the depleting zones, CS is probably more abundant than SO. To check this point we have compared the SO and CS integrated intensities, and the ratio of

As shown in Fig. 3 of Paper I, the cosmic background is no longer negligible if the excitation temperature is close to 2.73 K, i.e. $T_{ex} \leq 5$ K, which is the case of most species with high dipolar momentum in the typical density range of dark clouds.
SO \((J_{K'}:3_{2}\rightarrow2_{1})\) to CS \((J_{2}:2\rightarrow1)\) line integrated intensities with \(A_V\) (Fig. 15). Both lines are emitted in regions with hydrogen density below their critical density and both lines are optically thick, implying that they are both proportional to their column density to a first approximation. There is a clear trend for SO to start at a comparable or slightly lower intensity than CS and, coming closer to the depleting core, to become more intense up to \(A_V = 15\) mag. This obviously requires a more quantitative evaluation.

4.4. N-bearing species

It has been recognized that N-bearing species like NH\(_3\) and N\(_2\)H\(^+\) should deplete only at very high densities, \(n > 10^6\) cm\(^{-3}\) (Bergin & Langer 1997), or even higher (e.g. \(n \geq 3 \times 10^5\) cm\(^{-3}\) according to Aikawa et al. 2003). The reason given is the lower binding energy for nitrogen with respect to carbon or oxygen. This ability to stay longer in the gas phase should make these species good mass tracers in the dark cloud cores. Furthermore deuterated N-bearing species should be even more efficient core tracers, deuteration being enhanced by the disappearance of CO (e.g., Caselli 2002; Bacmann et al. 2003). However some question has arisen as to whether these species should eventually also start depleting in the densest, coldest pre-stellar cores as reported by Bergin et al. (2002). We have thus compared our N\(_2\)H\(^+\) \((J_{1}:1\rightarrow0)\), N\(_2\)D\(^+\) \((J_{2}:2\rightarrow1)\) and \((J_{3}:3\rightarrow2)\) and the para-NH\(_3\)D \(J_{KK':11\rightarrow10}\) data of Tiné et al. (2000) to our dust map (Fig. 8).

4.4.1. N\(_2\)H\(^+\)

The N\(_2\)H\(^+\)/\(A_V\) comparison (Fig. 16a) shows that N\(_2\)H\(^+\) appears above \(A_V \approx 10\) mag only and also shows signs of depletion above \(A_V \approx 50\) mag. The north-south cut across the main dust peak (Fig. 9) also suggests depletion (more correctly, the depletion concerns the parent species of N\(_2\)H\(^+\), N\(_2\), as the ion cannot stick to grains itself). However the line is strongly saturated as the spectrum taken towards the dust peak shows (Fig. 17) and it could be argued that the saturation above \(A_V \approx 50\) mag in Fig. 16a comes from opacity effects. To check this point, we have studied the \((J_{F,F':11\rightarrow01})\) line and estimated its opacity using the CLASS HFS method\(^4\). We find total opacities (sum of the opacities of all the 7 hyperfine transitions of the \(J_{1}:1\rightarrow0\) line) in the range 10–30 mostly, yielding \((J_{F,F':11\rightarrow01})\) opacities in the range 0.4–1.1. This is the weakest and the only optically thin hyperfine transition for this \((J_{1}:1\rightarrow0)\) line and this range of total opacities. We have also compared its integrated intensity to \(A_V\) (Figs. 9 and 16b). In Fig. 16b, the results are comparable to those obtained for the total integrated intensity (Fig. 16a) but the result is less convincing when we look at a few points (Fig. 9). One should note however that this particular hyperfine transition suffers from noticeable excitation temperature deviations (Caselli et al. 1995) which could explain such a difference on a few data points. In any case, the north-south cut of the \((J_{F,F':11\rightarrow01})\) transition does not reveal the dust peak and in conclusion, optical thickness cannot explain our results. Depletion of N\(_2\) is the only possibility left.

To evaluate the range of densities where N\(_2\)H\(^+\) is present, we can try to analyze the N\(_2\)H\(^+\) spectra with CLASS HFS method combined with a crude non-LTE (LVG) analysis of the physical conditions, using Green’s collision coefficients (which do not take into account the hyperfine splitting, Green 1975). In the case of the spectrum taken towards the dust peak (Fig. 17), we get a total opacity of \(\sim 20\) (i.e. individual hyperfine component opacities from 0.8 to 5), an excitation temperature of 4.6 K and a remarkably narrow linewidth (0.18 km s\(^{-1}\)). Considering a single hyperfine transition as an isolated line, the LGV model indicates a local density of \(\sim 2.5 \times 10^4\) cm\(^{-3}\) and a total column density of \(\sim 10^{13}\) cm\(^{-2}\) if we suppose the kinetic temperature to be 10 K. If we try to fit the \((J_{F,F':11\rightarrow01})\) transition, we find a density \(\sim 8 \times 10^4\) cm\(^{-3}\) instead, and towards

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\(^4\) The Grenoble data reduction package. The HFS method assumes LTE holds among the hyperfine components which is approximate in the case of N\(_2\)H\(^+\) \((J_{1}:1\rightarrow0)\) (Caselli et al. 1995).
we have found for cm is b) 2′ F 2 × ffiffi ffi = appears where CO disappears. Towards jn Fig. 3 of Paper II. Because the dust peak maximum density increases by a factor of ±5 following the density profile of Paper II (their Fig. 3). In first approximation, the intensity of the line is proportional to its column density (CD) and to the gas density, n(H2), as long as the gas density is below the critical density for the transition we observe. This has been checked with an LGV model for the N2D+ (J:3−2) line and the range of other places in the cloud, where the N2H+ line is not so optically thick, the same crude LGV analysis yields densities around 10^5 cm^{-3}. It thus indicates that towards the main dust core we are mostly measuring the outer parts of the N2H+ region where the density is low. This is due to the fact that the escaping photons are those emitted in the last absorbing layer outside the core, the one with the lowest density as the core density decreases radially (Paper II). This density of 2.5 × 10^4 cm^{-3} is consistent with the density of 3 × 10^5 cm^{-3} we have found for C^{18}O and CS (Paper I) together with the fact that CO and N2H+ cannot coexist: N2H+ appears where CO disappears. Towards the center, it is difficult to evaluate precisely at which density the ion starts to disappear by depletion but the turn-over point at Av ≈ 50 mag in Fig. 16 corresponds to a density of ~4 × 10^6 cm^{-3} in Fig. 3 of Paper II. Because the dust peak maximum density is 2 × 10^6 cm^{-3}, we can, conservatively, claim that N2H+ depletion starts below or close to 10^6 cm^{-3} and probably up to a factor of 2 lower.

4.4.2. N2D+ and NH2D

Another way to check the opacity problem is to look at the rarer isotopomer N2D+. Interestingly enough, the [N2D⁺]/[N2H⁺] abundance ratio is very high towards molecular peak C, ∼0.35 (Tiné et al. 2000). This large deuteration enhancement has been seen for many species in CO depleted cores (including ND3 in B1, Lis et al. 2002; and CD3OH in IRAS 16293−2422, Parise et al. 2004) and is clearly linked to the large depletion of heavy species (see, e.g., Roberts et al. 2003).

Despite its relatively high abundance, the N2D+ high electric dipole moment makes it difficult to populate the J = 2 rotational level of this species in cold, moderately dense dark cloud cores and thus the (J:3−2) transition is probably optically thin or close to optical thinness in the present source. Because the case is not so straightforward for the (J:2−1) transition and for the para-NH2D(J:11−10) transition, we have selected optically thin hyperfine components of both species to see if the maps were different and if we could find the dust peak. We find that the maps of the selected hyperfine components are identical (within the noise) to the maps presented here (Fig. 8). This can be seen in Fig. 9 where the optically thin component integrated intensities trace the same profile as the total integrated intensities for these two lines. In Fig. 8, we see the molecular peak 30′ north of the dust peak and a small extension to the dust peak for both NH2D and N2D+ but the dust peak is clearly absent. Thus it does not seem possible to find any species to trace the dust peak except H2D+ which has been recently discovered in L1544 (Caselli et al. 2003) and also towards this source (Caselli et al. in preparation) and, with even greater observing difficulties, D2H+, recently discovered in 16293E (Vastel et al. 2004).

From the molecular peak to the dust peak, the dust column density increases by a factor of ∼1.5 and the peak density by a factor of ∼5 following the density profile of Paper II (their Fig. 3). In first approximation, the intensity of the line is proportional to its column density (CD) and to the gas density, n(H2), as long as the gas density is below the critical density for the transition we observe. This has been checked with an LGV model for the N2D+ (J:3−2) line and the range of...
densities implied here. The intensity of the line is thus proportional to the integral along the line of sight of the product CD × n(H₂). This integral increases by a factor ~4 from the molecular peak to the dust peak, while the N₂D⁺ (J=3–2) line integrated intensity is approximately constant. Therefore, the line hyperfine components being close to optical thinness, we must conclude that the line of sight depletion reaches ~4 compared to the molecular peak. Consequently, the volume depletion must be at least a factor of ~15 for these N-bearing species on average if we suppose that we may have missed a 20% (3σ) intensity increase from molecular peak to dust peak in our observations (we expect a factor 4 increase and we may have only 1.2, (4−1)/(1.2−1) = 15, the ~1 is due to the undepleted part in front and behind the core⁵).

Instead of depletion, one could argue that the molecular peak is peculiar with a strong N₂D⁺ enrichment. In fact, Fig. 9 reveals that N₂D⁺ and NH₂D do follow the dust profile on both sides of the dust peak and that the molecular peak existence and asymmetry with respect to the dust peak are due in fact to the asymmetric dust profile itself. The molecular peak lies on the northern ridge (Pagani et al. 2003; Paper II) at the closest position to the core before depletion sets in. Because of the elongated ridge with a slow density variation, the region of high density without depletion is large enough to stand out as a molecular peak. In all the other directions away from the dust peak, the density drops much faster and therefore the region of maximum density without depletion is too narrow to be revealed. The column density has somewhat the same effect but to a lesser extent as we have seen above (the density changed by a factor 5 while the column density by a factor 1.5 between molecular peak C and dust peak 1). Therefore, the molecular peak is indeed displaced to the north by 30″ due to depletion.

4.5. Depletion trigger

Until now, it has not been clear whether the main trigger for depletion of species such as CO and CS is dust opacity (i.e. protection against evaporation by UV radiation) or density (i.e. speed of depletion). It seems from this study that density is the major trigger as the most detailed studies published today quote densities of the order a few 10⁴ cm⁻³ very close to our own value of 3 × 10⁴ cm⁻³ which is the density we have found in Paper I to explain C₁⁸O, C₃₂S and C₃⁴S line intensities towards the reference position. Tafalla et al. (2002) find 3–6 × 10⁴ cm⁻³, Tafalla et al. (2004) find 2.5 and 7.8 × 10⁴ cm⁻³, and Jørgensen et al. (2004) find 3 × 10⁵ cm⁻³. On the contrary, optical extinction thresholds are usually found close to AV = 10 mag (see Sect. 4.1) while we report AV = 20 mag here (and this is not even sufficient for peak 5–peak E which shows no depletion). Moreover we have recently found in a cloud in the Taurus region C₁⁸O depletion starting at AV ~ 4 mag, the lowest AV value presently known for CO depletion (Boudet et al., in preparation).

Concerning the two important nitrogen-bearing species (N₂H⁺ and NH₃, the latter being represented by its deuterated isotopomer NH₂D only), we find that they are depleted at densities somewhere between 5 × 10⁵ and 10⁶ cm⁻³. While Bergin & Langer (1997) predict such an effect at this density level for grains covered by polar (H₂O) ices, a more recent paper (Aikawa et al. 2003) estimates that N₂H⁺ and NH₃ depletion is unlikely below densities of 3 × 10⁶ cm⁻³. The possible reason which they invoke for this effect is that the binding energy of N₂ onto grains could be lower than usually advocated (a similar effect is found by Bergin & Langer 1997, for grains with no ice or apolar (CO) ice). The present result would tend to show that the polar ice case described by Bergin & Langer (1997) is probably closer to the truth.

4.6. The peak E case

Despite a peak visual extinction of ~25 mag (Paper II), Peak E shows no CO depletion and correlatively very weak N₂H⁺ emission. This peak is in fact the C₁⁷O and C₁⁸O emission peak of the whole cloud. This peak is also a 100 and 200 µm peak (Paper I) from which we have derived an average temperature of ~15 K. However, this temperature yields a 200 µm-derived dust extinction AV ≈ 7 mag (Paper I) too low compared to the NIR-determined visual extinction (Paper II). This probably indicates that the bulk of the dust is at a lower temperature and that some layers are at higher temperatures than 15 K. These warm layers would not allow depletion of apolar molecules like CO but their total opacity being low, they cannot account for all the C₁⁸O emission detected. In Paper I, we have tried to fit the C₁⁸O (J=1−0), (J=2−1) and (J=3−2) rotational line emission with a Monte-Carlo code. Although we somewhat failed to reproduce the very low (J=2−1) line emission, we are probably close to the solution, in terms of the column density estimate which is 3.5 × 10¹⁵ cm⁻². Compared to a peak AV of ~25 mag, this yields an abundance of ~1.4 × 10⁻⁷, which is the standard value recommended by Frerking et al. (1982). We have only weak C₁³S (J=2−1) line detections towards peak E in sharp contrast with C₁⁸O intensity. Though it is yet difficult to derive a density from a single CS transition, keeping the same C₁³S/C₁⁸O abundance ratio as measured towards the reference position (i.e. ~0.005) we find that C₁³S (J=2−1) and C₁⁸O (J=1−0), (J=2−1) and (J=3−2) are reasonably compatible with a core density of ~10¹⁴ cm⁻³. Thus, density could again be the explanation for the absence of depletion towards Peak E. Why this peak is less dense and (partially but substantially) warmer than the other peaks in this cloud is not yet clear.

In both Figs. 11 and 13, there is a drop (~30%) of intensity with respect to C₁⁸O for the last averaged point (corresponding to the strongest C₁⁸O emission). This average point contains only C₁⁸O positions in the direction of peak E. As we have seen above, the C₁⁸O abundance is normal towards peak E, and we could find the same C₁³S/C₁⁸O abundance ratio as measured towards the reference position provided that the peak density be no higher than ~10¹⁴ cm⁻³. Though we cannot do a similar excitation analysis for SO, it is most

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⁵ A more accurate analysis will be performed in a coming paper when the detailed collisional coefficients (including hyperfine structure) of N₂H⁺ will be completely computed (Daniel et al. 2003; Daniel et al. in preparation).
probable that the intensity drop is also explained by the sole density factor. Thus the peak E is probably no peculiar regarding the species abundances. The question then arises of whether the weak N2H+ line observed in that direction is due to chemical destruction as predicted by models or only to the fact that the density is so low that it cannot be observed. The N2H+ line we have detected is so weak (~0.15 K (4σ)) that only the strongest component (J_F=1;132–0;12) emerges from the noise and no CLASS HFS analysis can be done. However, we know the density to be probably no more than 10^4 cm^-3 and therefore we can use the LVG code to crudely estimate the N2H+ column density. With T_{kin} = 10 K, we find a (J_F;F=1;132–0;12) line column density of 3 × 10^{11} cm^-2 which yields a total column density of ~1.2 × 10^{12} cm^-2. Compared to the dust extinction of 25 mag towards peak #5, we find a N2H+ abundance of 5 × 10^{-11}. If we repeat the same analysis for a few N2H+ observations towards lines of sight with ~40 mag of extinction (to stay away from both the depletion threshold and the threshold of destruction by CO), we find an abundance of 1.2–2.1 × 10^{-10}, 2 to 4 times higher towards peak E. Therefore, a low volume density is not the unique reason for the quasi-absence of N2H+ emission towards peak E. It has also an abundance lower than in the CO depleted region. Several theoretical and observational studies have shown that N2H+ appears in the gas when CO depletes (Bergin & Langer 1997; Bergin et al. 2001; Caselli 2002; Aikawa et al. 2003; Jörgensen et al. 2004). This analysis would appear to again confirm this effect.

5. Conclusions

All species containing at least one atom of the CNO group are depleted in the most inner core of L183. CO, CS and SO are largely depleted but their depletion starts only at a relatively high optical extinction (A_V ≈ 20 mag) unseen elsewhere. On the contrary, the density (n ≈ 3 × 10^4 cm^-3) for which depletion starts is similar to other findings and this result points towards the fact that density is the main parameter to trigger depletion rather than protection against UV radiation. Depletion effects, reported now in many dark clouds, prevent CO from being an accurate mass tracer for cold dense cores, and forbid the search of such cores via its rarer isotopomers (C^{17}O, C^{18}O). Similarly, CS is not a good density tracer in many cold clouds because it survives in the gas phase only at densities much below its critical density and thus its intensity is mostly proportional to its column density. N-bearing species (especially N2H+ and NH3) are better tracers of dense cores but only up to densities below 10^9 cm^-3. Beyond that limit, they also disappear (Bergin et al. 2001). Like for L1544 and 16293E, only HD^+ (Caselli et al. 2003) and D2H+ (Vastel et al. 2004) should be observable in the inner core (Caselli et al., in preparation).

Finally, species abundances for chemical models such as those provided by Dickens et al. (2000) for L183 are meaningless averages along the line of sight of species which are not necessarily coexistent spatially. Only models including geometry, depletion and radiation transport can nowadays be usefully compared to the detailed observations allowed by modern telescopes. Such models have recently been proposed by Bergin et al. (2001, including a chemical network scheme) or by Jörgensen et al. (2004) and similar studies in protostellar cores have been presented by Tafalla et al. (2002, 2004).

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References

Caselli, P. 2002, P&SS, 50, 1133
Penzias, A. A. 1975, in Atomic and molecular physics and the interstellar matter; Proceedings of the Twenty-sixth Summer School of Theoretical Physics, Les Houches, France, July 1–August 23, 1974 (Amsterdam: North-Holland Publishing Co.), 373
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Appendix A: Subthermally excited optically thick lines

A radiotelescope which observes a source with opacity \( \tau \) and excitation temperature \( T_{\text{ex}} \) by comparison with an empty field, detects an antenna temperature \( T_a \) increase given by

\[
\Delta T_a = \eta (1 - e^{-\tau}) (J(T_{\text{ex}}) - J(T_{\text{bg}}))
\]  

(A.1)

with \( \eta \) the coupling efficiency of the telescope, \( T_{\text{bg}} \), the temperature of the cosmological background radiation and \( J(T) \) is given by

\[
J(T) = \frac{h \nu}{k} \frac{1}{\sqrt{\pi}} - 1
\]  

(A.2)

where \( h \) is the Planck constant, \( k \) the Boltzmann constant and \( \nu \) the line frequency. When \( \tau \gg 1 \), Eq. (A.1) simplifies to

\[
\Delta T_a = \eta (J(T_{\text{ex}}) - J(T_{\text{bg}}))
\]  

(A.3)

which would seem to be independent of \( \tau \) and therefore of the species column density as \( \tau \) is defined by

\[
\tau = \frac{c^2 g_u A_{ul} N_l}{8 \pi g_l \nu^2 \Delta \nu} \left[ 1 - e^{-\frac{h \nu}{kT}} \right]
\]  

(A.4)

with \( c \) the light speed, \( A_{ul} \) the Einstein spontaneous emission coefficient, \( g_u \) and \( g_l \) the upper and lower species level statistical weights and \( N_l \), the lower level column density. The latter is related to the total column density via the partition function.

In fact, when a line is optically thick and the local density is much below the critical density (defined by \( n_{\text{crit}} = A_{ul}/\gamma_{ul} \), \( \gamma_{ul} \) being the collision probability), each exciting collision has a higher probability to be followed by a radiative decay rather than a collisional deexcitation. But similarly, if the photon is reabsorbed because of high opacity, it will still be reemitted rather than having the species be deexcited by a collision. Thus each exciting collision will give birth to a photon which will eventually escape. If the opacity is high, many photons are retained in the cloud before escaping and the net result is an increase of the excitation temperature and therefore of the antenna temperature in Eq. (A.3). We refer the reader to Penzias (1975) or Linke et al. (1977) for a mathematical demonstration. Here we want to illustrate this result via two simulations and actual observations.

Figures A.1 and A.2 show the case of \(^{32}\text{S} \,: J(1 \rightarrow 0) \) and \( J(2 \rightarrow 1) \) lines in a very low density medium (\( 10^3 \text{ cm}^{-3} \)) and at two different kinetic temperatures (Fig. A.1, \( T_{\text{kin}} = 10 \text{ K} \), Fig. A.2, \( T_{\text{kin}} = 50 \text{ K} \)). The line opacity and antenna temperatures are proportional to the total column density below \( N = 10^{13} \text{ cm}^{-2} \), which corresponds to \( \tau \ll 1 \) and \( T_{\text{ex}} \) is almost constant. Above \( N = 10^{13} \text{ cm}^{-2} \), i.e., \( \tau \gg 1 \), the excitation temperature starts to rise and the antenna temperature keeps increasing linearly first then deviates while approaching the excitation limit (collisional deexcitation starts to become efficient when too many molecules are in the excited state).

In L183, the \( \text{N}_2\text{H}^+ \, J(1 \rightarrow 0) \) line has the advantage of having both a hyperfine transition always optically thin \( (J_{F,F':11-00}) \) and another one, almost always optically thick \( (J_{F,F':23-02}) \) in the range of conditions offered by this cloud. The line has a critical density around \( 10^6 \text{ cm}^{-3} \) and is therefore subthermally excited everywhere in the cloud. Figure A.3 shows the comparison of the two hyperfine transition integrated intensities together with the 1:7 slope corresponding to their LTE ratio. The proportionality is clearly visible despite a slight departure from the 1:7 slope. This departure is probably due to the emergence of a saturation effect or to the fact that the \( (J_{F,F':11-00}) \) line often departs from the LTE ratio (Caselli et al. 1995).
Fig. A.3. Comparison of the $N_2H^+$ $(J_{F_F':110-001})$ and $(J_{F_F':123-012})$ line integrated intensities. Square symbols identify those spectra for which the $(J_{F_F':123-012})$ line is optically thin. Low signal-to-noise ratios explain the presence of “optically thick” crosses in the bottom left corner.