



# Interstellar reddening correction using HeI lines

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**ESTALLIDOS 7.0**  
**Starburst along the life of the Universe**



## Interstellar extinction

- Interstellar extinction is generated by the scatter and absorption of photons by the medium between the observer and the radiation source.
- It is produced by dust grains and gas present in the interstellar medium and this mechanism is effective in photons with wavelengths comparable to the size of grains.
- The correction of the observed line fluxes for this effect is an indispensable preliminary step for the physical interpretation of the data.



## Methods to determine interstellar extinction

- Using the ratio of two forbidden lines from the same upper set of levels.
- Comparing hydrogen recombination lines from two different series arising from the same upper level.
- Comparing two hydrogen recombination lines from the same series, even if they do not originate from same upper level.

**The use of these strong lines can lead to selection biases when studying regions with different surface brightness**

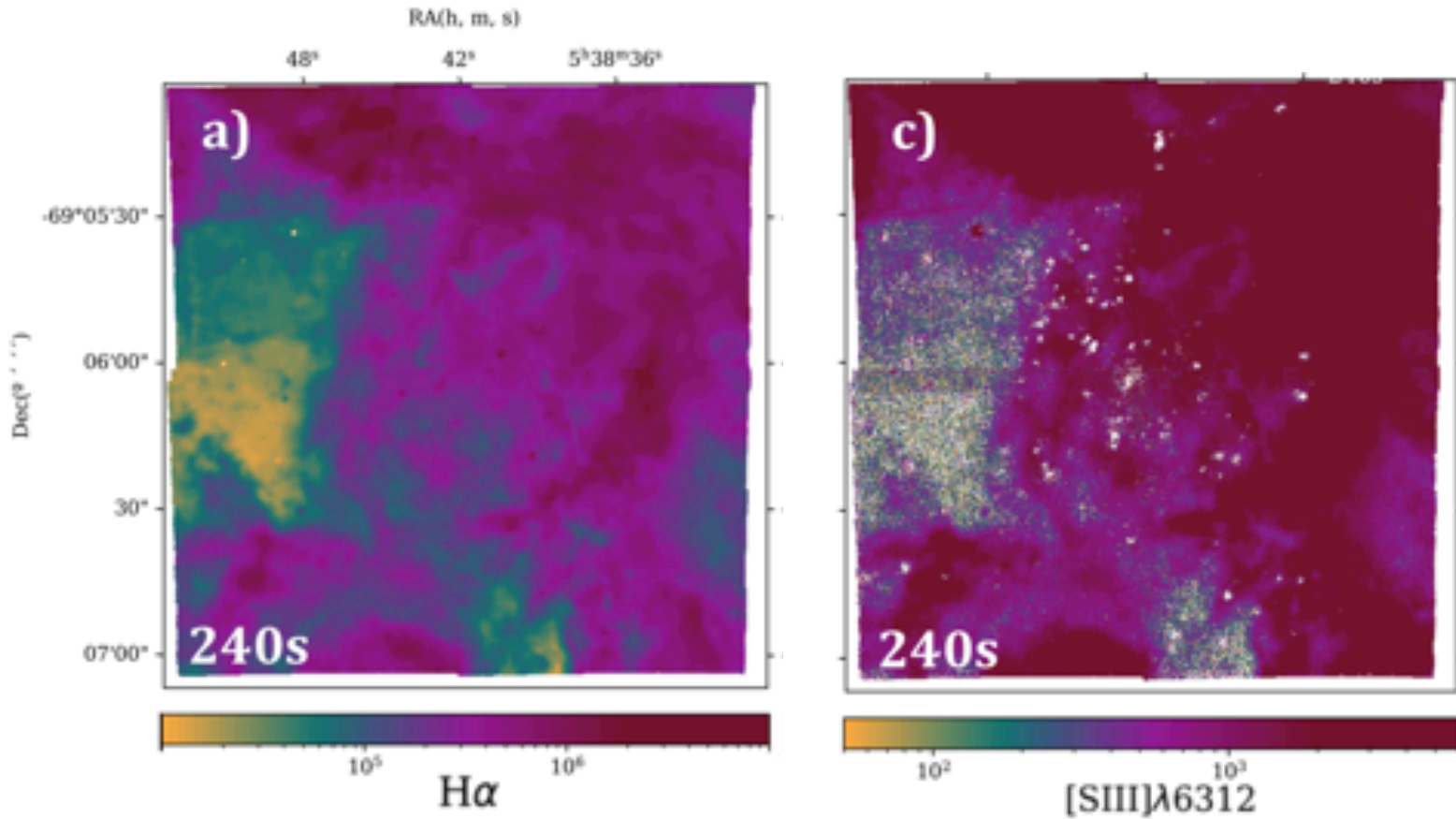


## H $\alpha$ /H $\beta$ disadvantages

- Some spectrographs not including these Balmer lines.
- In extended nebulae observations are focused only in the brightest region.
- In Integral Field Spectroscopy data, we can study physical conditions of the entire nebula but cover a very large dynamical range of surface brightness.

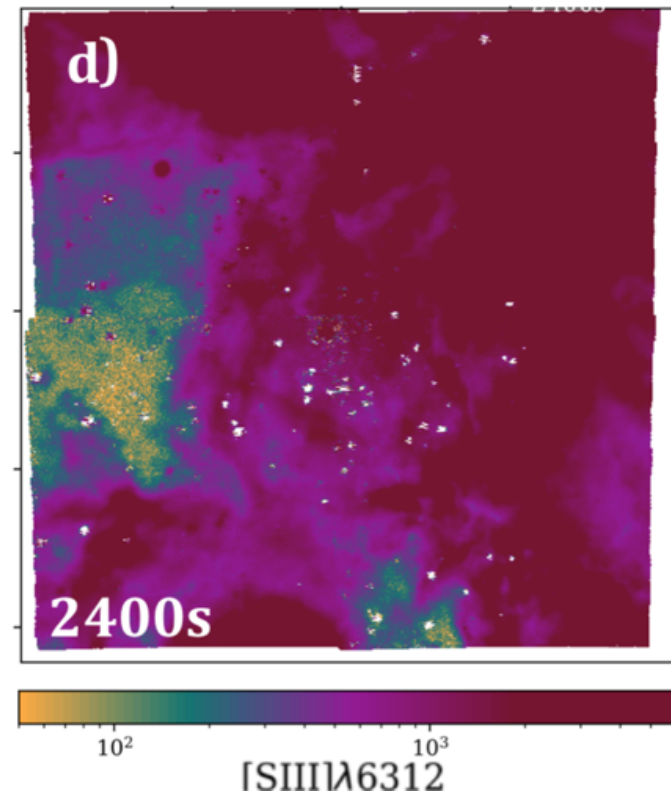
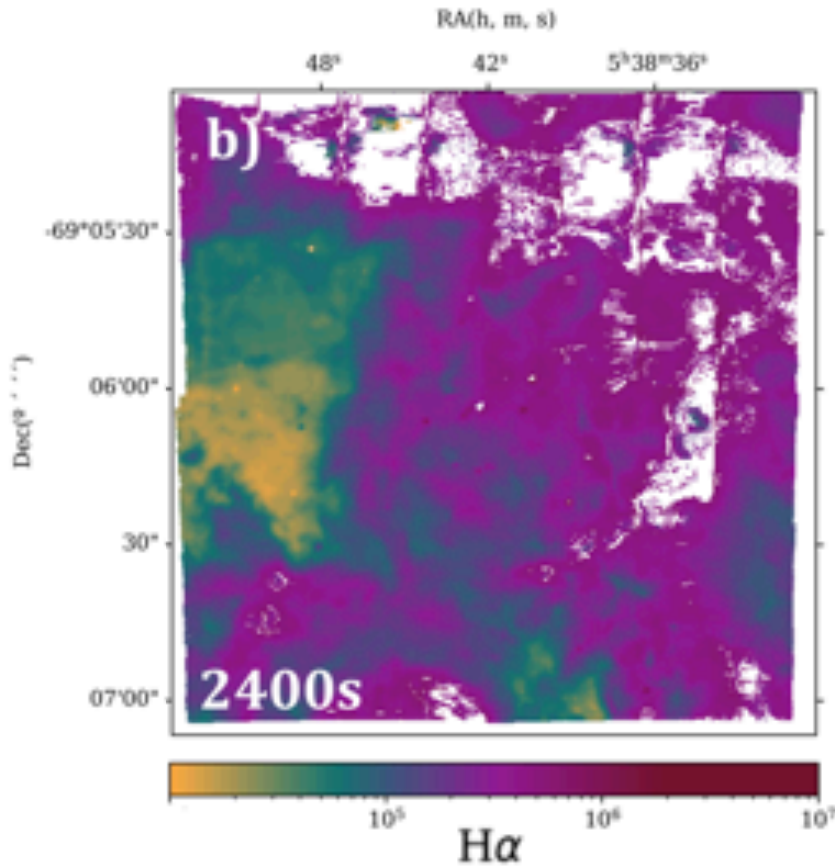


## H $\alpha$ /H $\beta$ disadvantages



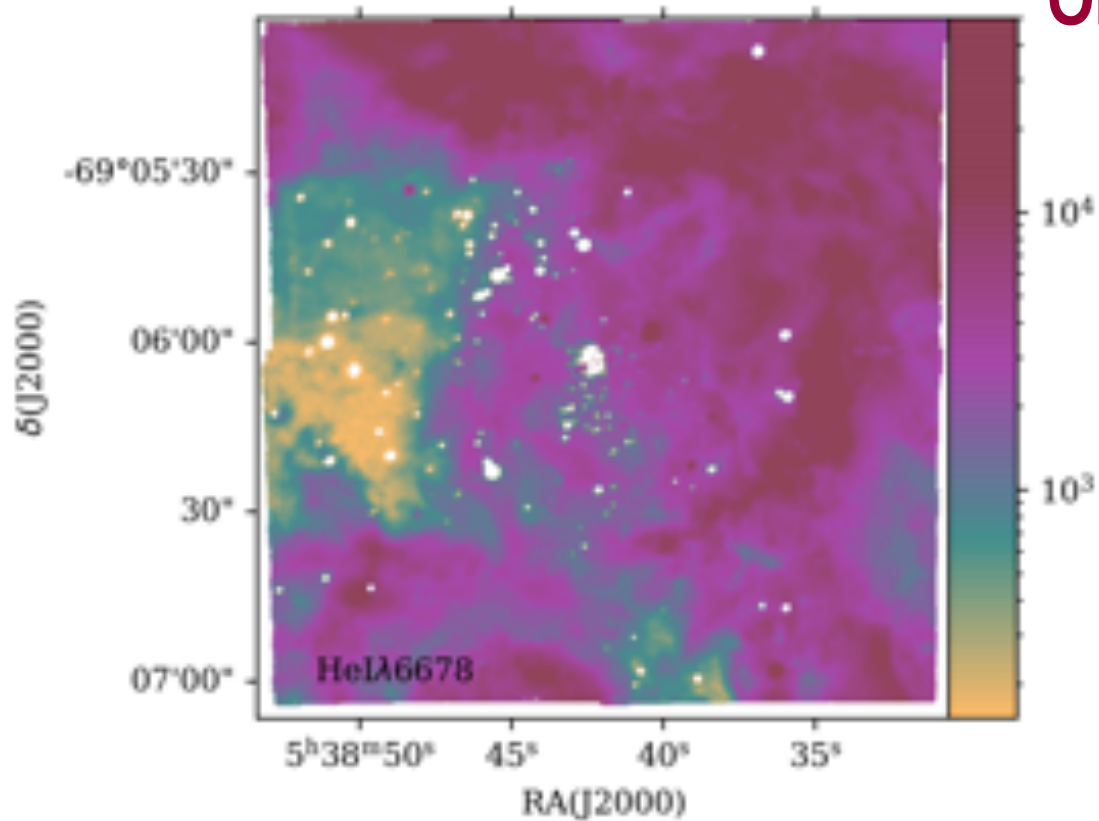


## H $\alpha$ /H $\beta$ disadvantages





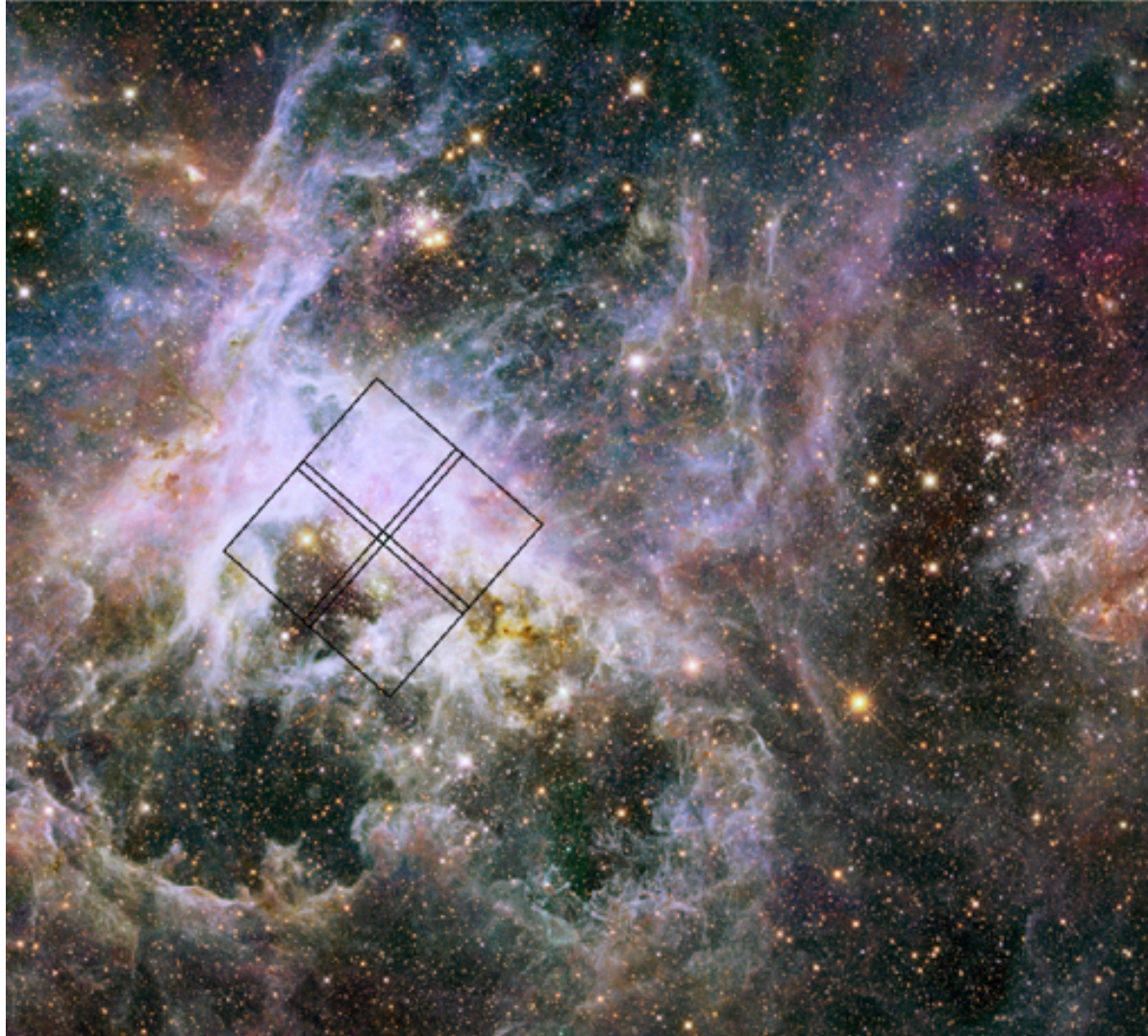
## Observations



- We propose an alternative method to derive extinction corrections **based on the lines of He.**



Wide Field Camera 3 (WFC3) y Advanced Camera for Surveys (ACS).  
Azul, banda I; verde, banda J; rojo, banda H







Wide Field Camera 3 (WFC3) y Advanced Camera for Surveys (ACS).  
Azul, banda I; verde, banda J; rojo, banda H

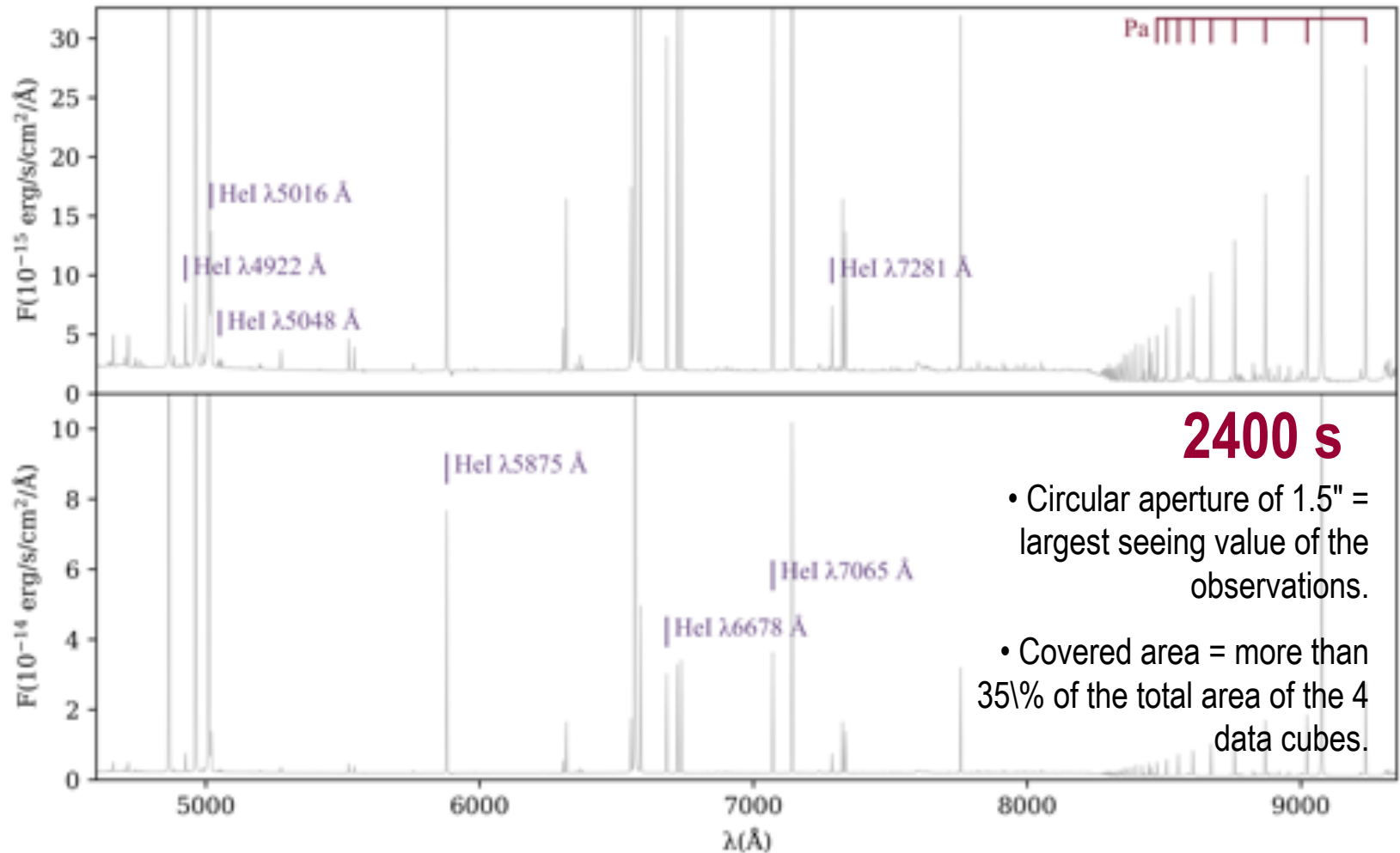


1x1 minarc<sup>2</sup> x 4 campos

**240 s y 2400 s**



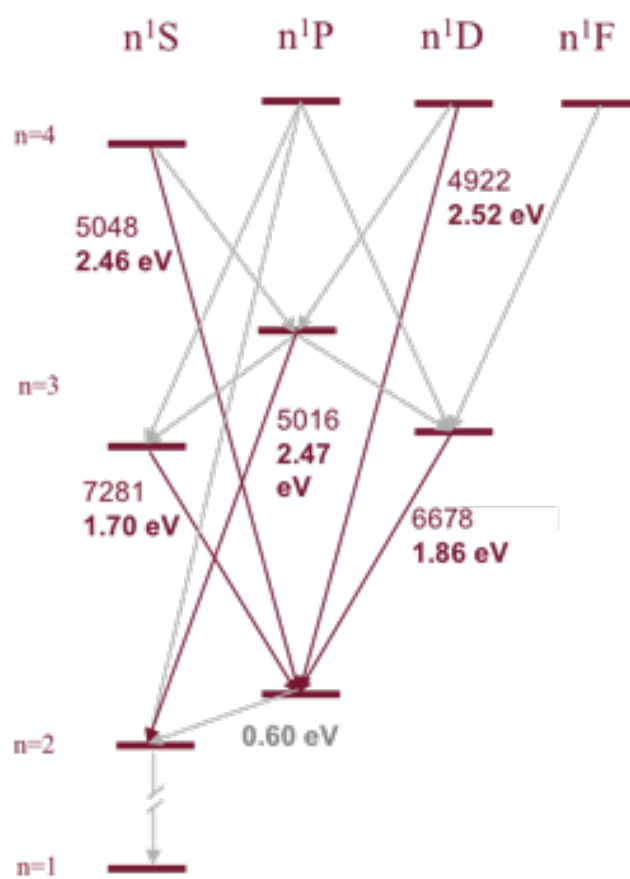
## Observations



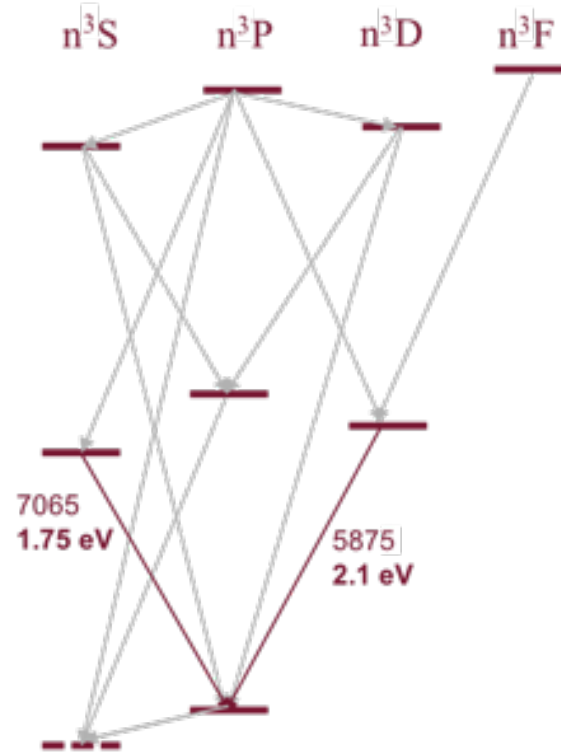


# Theoretical context

## SINGLET

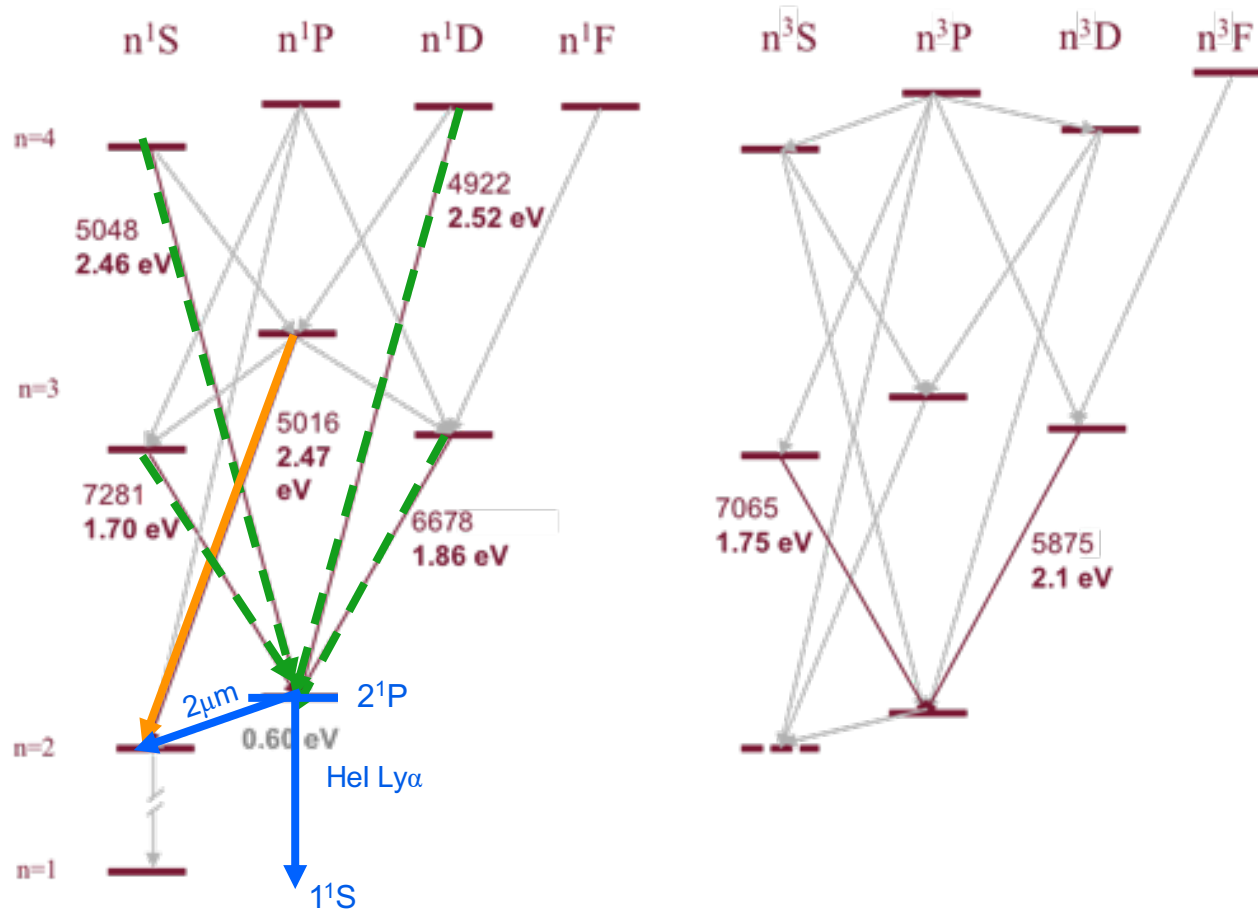


## TRIPLET



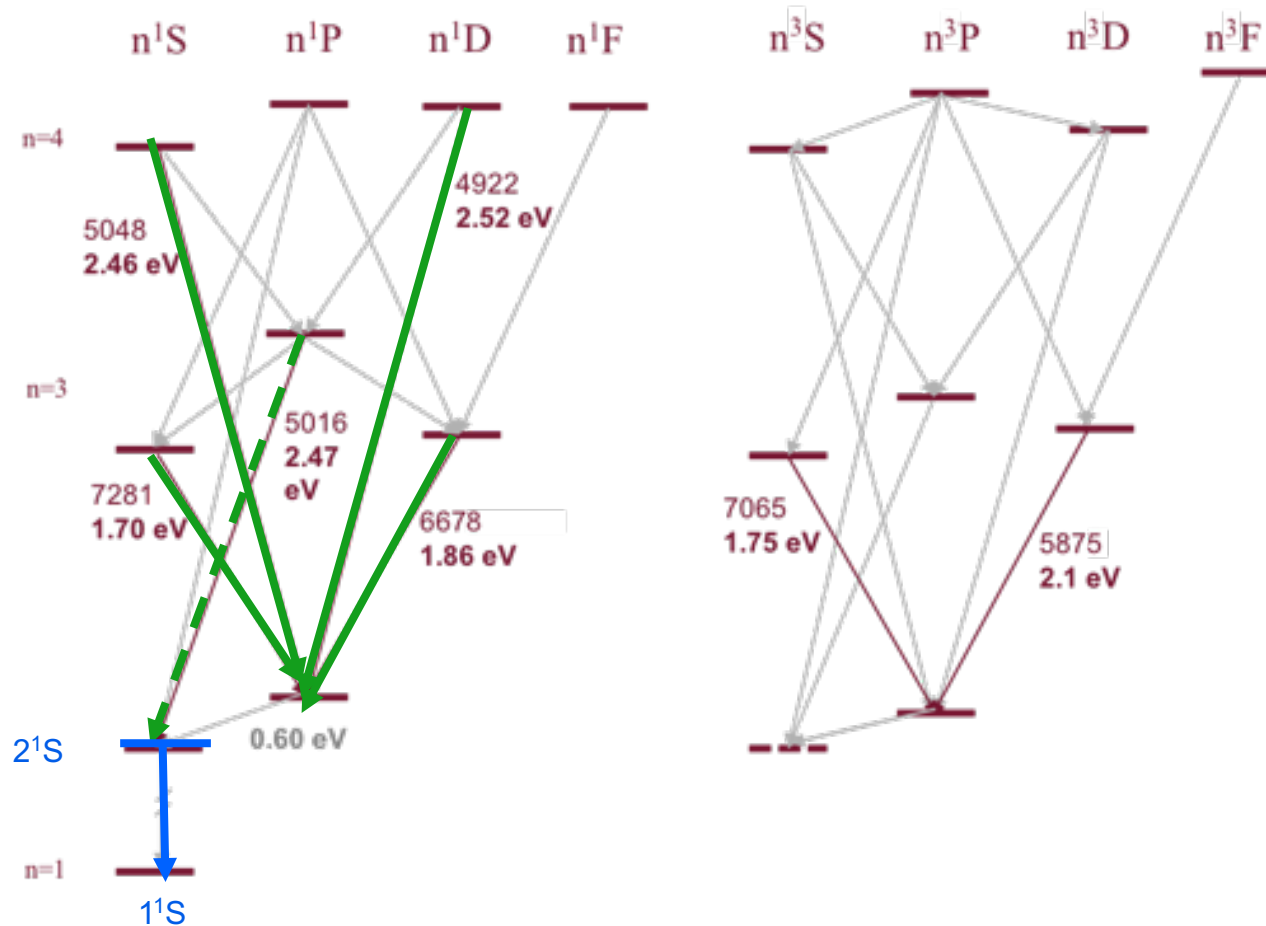


## Singlet states



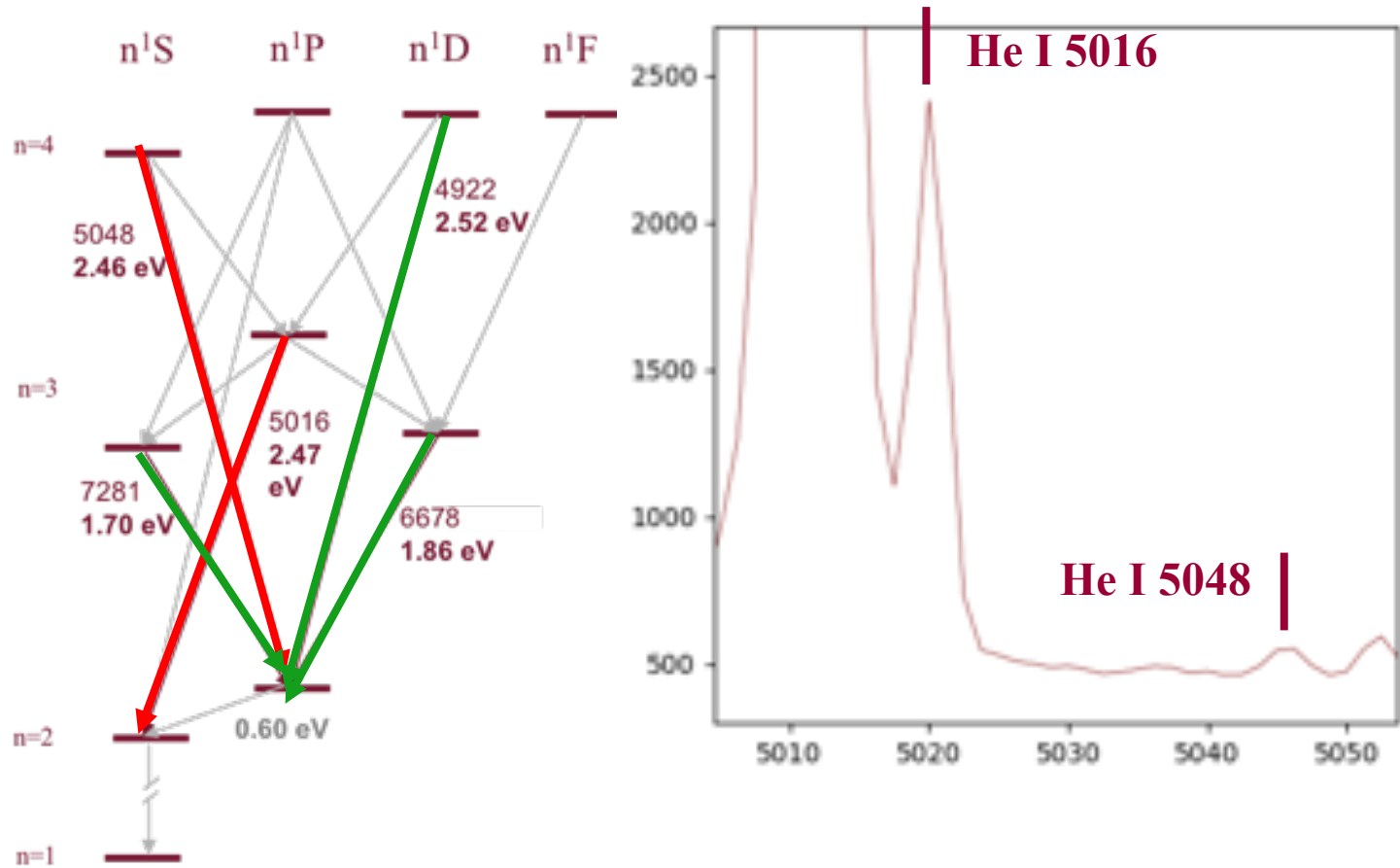


## Singlet states



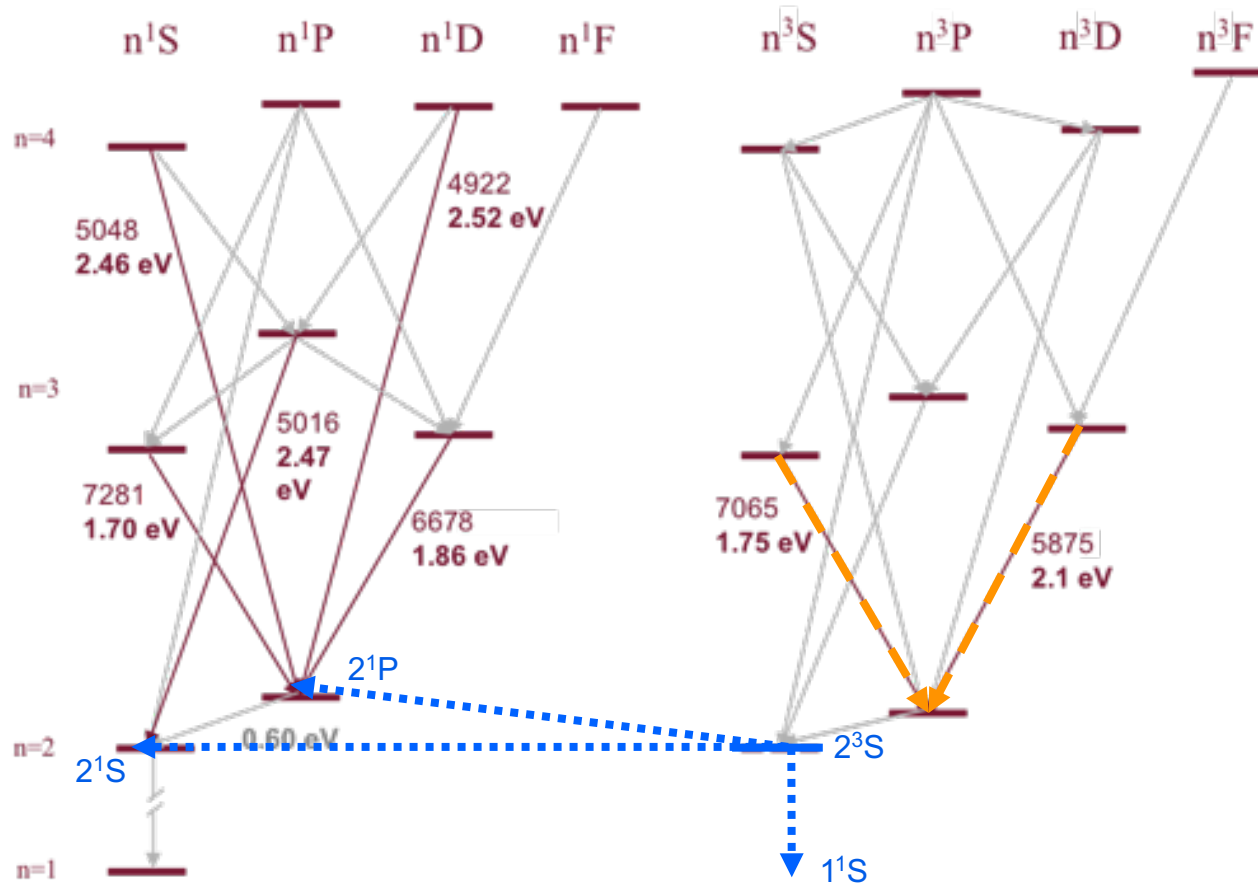


## Singlet states





## Triplet states





# Collisional contribution

TABLE 8  
POPULATIONS OF METASTABLE  $2^3S$  AND  $2^1S$  AND RESULTANT COLLISIONAL CONTRIBUTIONS ( $T = 20,000$  K)<sup>a</sup>

COLLISIONAL-TO-RECOMBINATION LINE CONTRIBUTION	$\log n_e = 2$		$\log n_e = 4$		$\log n_e = 6$	
	BSS <sup>b</sup>	KF <sup>c</sup>	BSS	KF	BSS	KF
$n(2^3S)/n_{\text{H I}}^{\text{d}}$	$1.03 \times 10^{-7}$	$1.06 \times 10^{-7}$	$2.04 \times 10^{-6}$	$2.02 \times 10^{-6}$	$2.53 \times 10^{-6}$	$2.46 \times 10^{-6}$
C/R(3890)	0.042	0.043	0.828	0.815	1.022	0.994
C/R(3189)	0.023	...	0.463	...	0.571	...
C/R(2946)	0.004	...	0.085	...	0.105	...
C/R(7067)	0.152	0.153	3.024	2.898	3.763	3.532
C/R(5877)	0.034	0.055	1.077	1.043	1.343	1.271
C/R(4715)	0.112	...	2.223	...	2.777	...
C/R(4473)	0.035	0.038	0.688	0.712	0.853	0.868
C/R(4027) <sup>d</sup>	...	0.019	...	0.358	...	0.436
C/R(18690)	0.018	...	0.355	...	0.448	...
$n(2^1S)/n_{\text{H I}}^{\text{e}}$	$7.57 \times 10^{-14}$	...	$2.32 \times 10^{-13}$	...	$2.71 \times 10^{-9}$	...
C/R(5017)	0.015	...	0.287	...	0.359	...
C/R(3966)	0.009	...	0.175	...	0.218	...
C/R(7283)	0.054	0.052	1.063	0.991	1.338	1.208
C/R(6630)	0.016	0.016	0.313	0.308	0.402	0.375
C/R(4923)	0.013	0.014	0.262	0.267	0.331	0.325
C/R(4389)	...	0.011	...	0.204	...	0.248
C/R(18701)	0.004	...	0.082	...	0.107	...

15%  
5%

<sup>a</sup> Only lines with collisional corrections, C/R, greater than 1% over the density range are shown.

<sup>b</sup> Current work.

<sup>c</sup> From Kingdon & Ferland 1995.

<sup>d</sup>  $2^1S$  population not estimated in Kingdon & Ferland 1995.

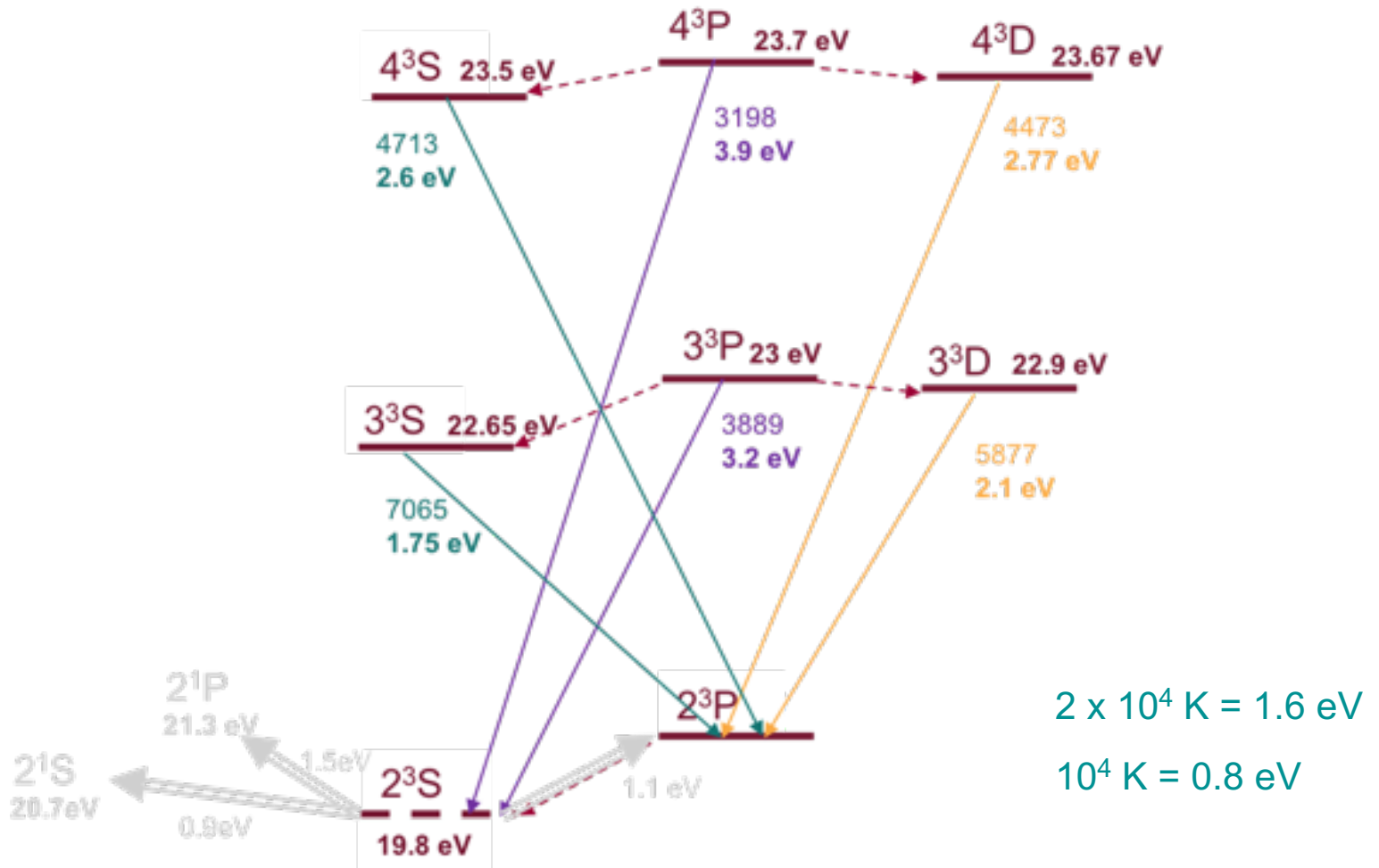
<sup>e</sup> Collisions to  $n = 5$  not included in current work. See § 3.1.

Robert A. Benjamin et al. 1999





## Radiative transfer



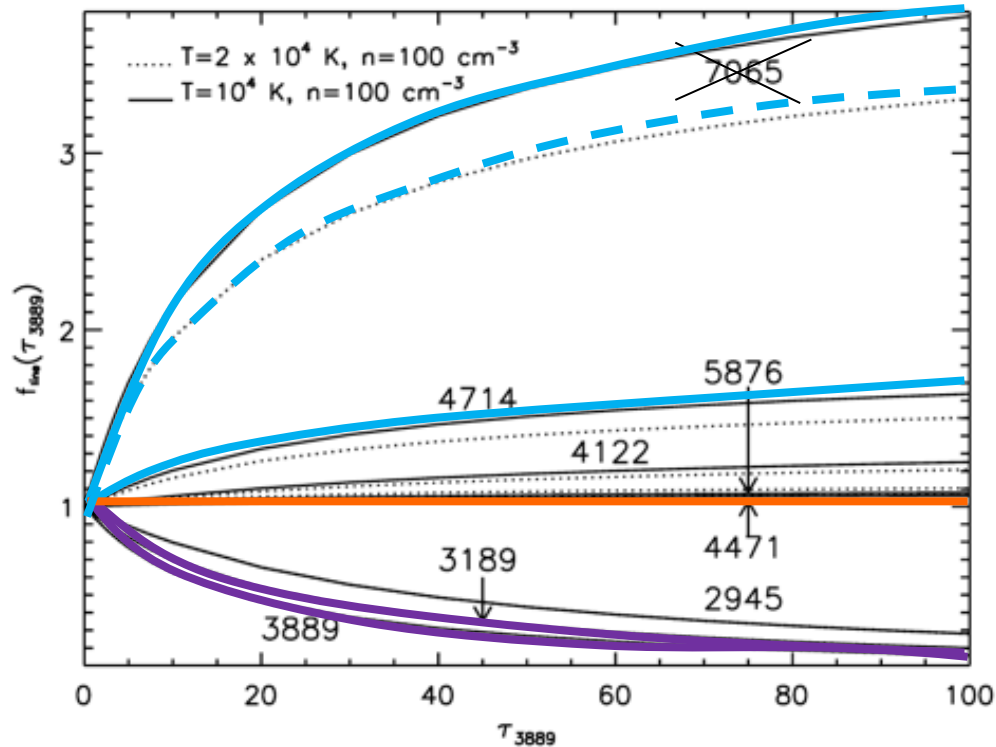


FIG. 2.—Optical depth correction factor for selected optical lines for cases with a particle density of  $n_H = 100 \text{ cm}^{-3}$  and two different temperatures.

Robert A. Benjamin et al. 2002

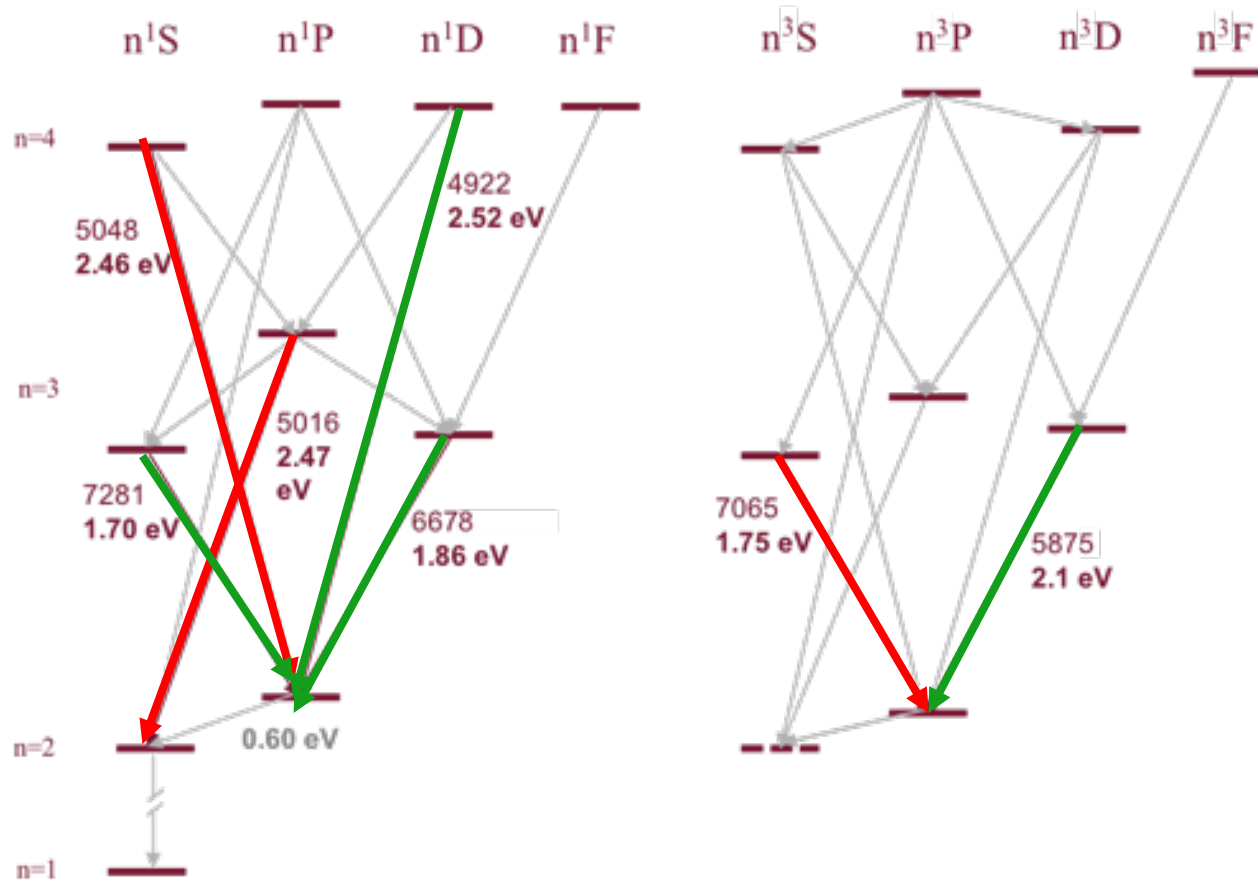
## Radiative transfer

$$2 \times 10^4 \text{ K} = 1.6 \text{ eV}$$

$$10^4 \text{ K} = 0.8 \text{ eV}$$



## Theoretical context





## Case B of recombination

The fluxes of two lines separated in wavelength are measured.

The most intense line of those left to us will be selected as a reference: **HeI 6678**

A typical ratio of these fluxes is assumed.

Pyneb, Luridiana et al. (2015)

Datos atómicos de

Storey & Hummer (1995) para H

Porter et al. (2012) para He

An extinction curve is assumed.

Miller & Mathews (1972),  $R_v = 3.2$

Line	$f(\lambda)^a$	$I_\lambda/I_{ref}^b$
H $\beta$	0	1.000
HeI $\lambda 4922 \text{ \AA}$	-0.014	0.345
HeI $\lambda 5875 \text{ \AA}$	-0.209	3.518
H $\alpha$	-0.313	2.863
HeI $\lambda 6678 \text{ \AA}$	-0.329	1.000
HeI $\lambda 7065 \text{ \AA}$	-0.377	0.621
HeI $\lambda 7281 \text{ \AA}$	-0.402	0.187
Pa17	-0.514	0.004
Pa16	-0.518	0.004
Pa15	-0.521	0.005
Pa14	-0.525	0.007
Pa13	-0.531	0.008
Pa12	-0.537	0.011
Pa11	-0.546	0.014
Pa10	-0.557	0.018
Pa9	-0.572	0.025

<sup>a</sup> Miller & Mathews (1972),  $R_v = 3.2$ .

<sup>b</sup> Luridiana et al. (2015),  $n_e(\text{cm}^{-3}) = 10^2$ ,  $T(\text{K}) = 10^4$ .

**Table 1.** Empirical values of the normalised logarithmic extinction at the wavelengths of the different HeI emission lines from Miller & Mathews (1972), and the ratio of these lines to the  $\lambda 6678 \text{ \AA}$  reference line as calculated by the PyNeb (Luridiana et al. 2015) tool for  $T = 10^4 \text{ K}$  and  $n_e = 10^2 \text{ cm}^{-3}$ , using Storey & Hummer (1995) and Porter et al. (2012) atomic data for hydrogen and helium respectively.



# 1-Interstellar extinction correction using the ratio of two recombination lines

Line	$f(\lambda)^a$	$I_\lambda/I_{ref}^b$
H $\beta$	0	1.000
HeI $\lambda 4922 \text{ \AA}$	-0.014	0.345
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$$c(H\beta) = -\frac{1}{f(\lambda) - f(H\beta)} \cdot \left[ \log \left( \frac{F_\lambda}{F_{H\beta}} \right) - \log \left( \frac{I_\lambda}{I_{H\beta}} \right) \right]$$

$$c(H\beta) = -\frac{1}{f(\lambda) - f(HeI\lambda 6678)} \cdot \left[ \log \left( \frac{F_\lambda}{F_{HeI\lambda 6678}} \right) - \log \left( \frac{I_\lambda}{I_{HeI\lambda 6678}} \right) \right]$$



## 1-Interstellar extinction correction using the ratio of two recombination lines

- Hydrogen reddening from short exposure spectra (240 s).
  - ❖ Mean relative errors in fluxes of  $H\beta$  line  $\rightarrow$  0.92%
  - ❖ Mean relative errors in fluxes of  $H\alpha$  line  $\rightarrow$  0.15%
  - ❖ Absolute mean error of  $c(H\beta)$   $\rightarrow$  0.02.
- Helium reddening from long exposure spectra (2400 s).
  - ❖ Mean relative errors in fluxes of  $HeI \lambda 5875$  line  $\rightarrow$  0.37%
  - ❖ Mean relative errors in fluxes of  $HeI \lambda 6678$  line  $\rightarrow$  1.37%
  - ❖ Absolute mean error of  $c(H\beta)$   $\rightarrow$  0.05.



## 2-Interstellar extinction correction using a linear regression

Line	$f(\lambda)^a$	$I_\lambda/I_{ref}^b$
H $\beta$	0	1.000
HeI $\lambda$ 4922 Å	-0.014	0.345
HeI $\lambda$ 5875 Å	-0.209	3.518
H $\alpha$	-0.313	2.863
HeI $\lambda$ 6678 Å	-0.329	1.000
HeI $\lambda$ 7065 Å	-0.377	0.621
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**Table 1.** Empirical values of the normalised logarithmic extinction at the wavelengths of the different HeI emission lines from Miller & Mathews (1972), and the ratio of these lines to the  $\lambda$  6678 Å reference line as calculated by the PyNeb (Luridiana et al. 2015) tool for  $T = 10^4$  K and  $n_e = 10^2 \text{ cm}^{-3}$ , using Storey & Hummer (1995) and Porter et al. (2012) atomic data for hydrogen and helium respectively.

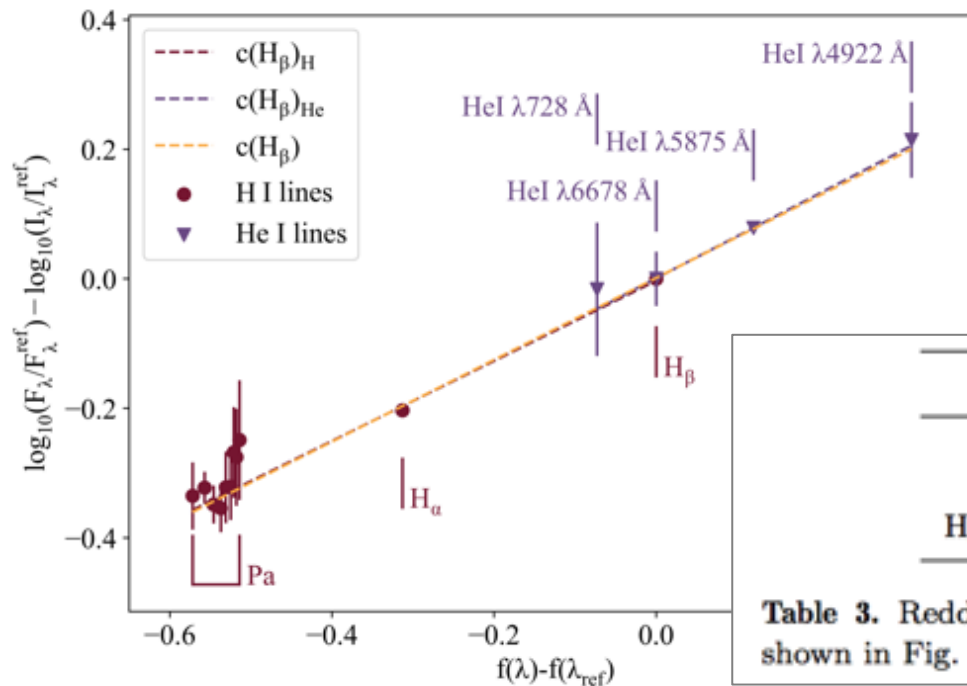
$$\log_{10} \left( \frac{F_\lambda}{F_{H\beta}} \right) - \log_{10} \left( \frac{I_\lambda}{I_{H\beta}} \right) = -c(H\beta)(f(\lambda) - f(H\beta))$$

$$\log_{10} \left( \frac{F_\lambda}{F_{HeI\lambda 6678}} \right) - \log_{10} \left( \frac{I_\lambda}{I_{HeI\lambda 6678}} \right) = -c(H\beta)(f(\lambda) - f(HeI\lambda 6678))$$



## 2-Interstellar extinction correction using a linear regression

The fits obtained for hydrogen lines, helium lines and all the lines together are consistent with each other and the intercept is compatible with zero.



Fit	$c(\text{H}\beta)$
Hydrogen	$0.619 \pm 0.018$
Helium	$0.650 \pm 0.050$
Hydrogen and Helium	$0.632 \pm 0.010$

**Table 3.** Reddening constant values obtained from the fitting shown in Fig. 4 for a randomly selected emission region.

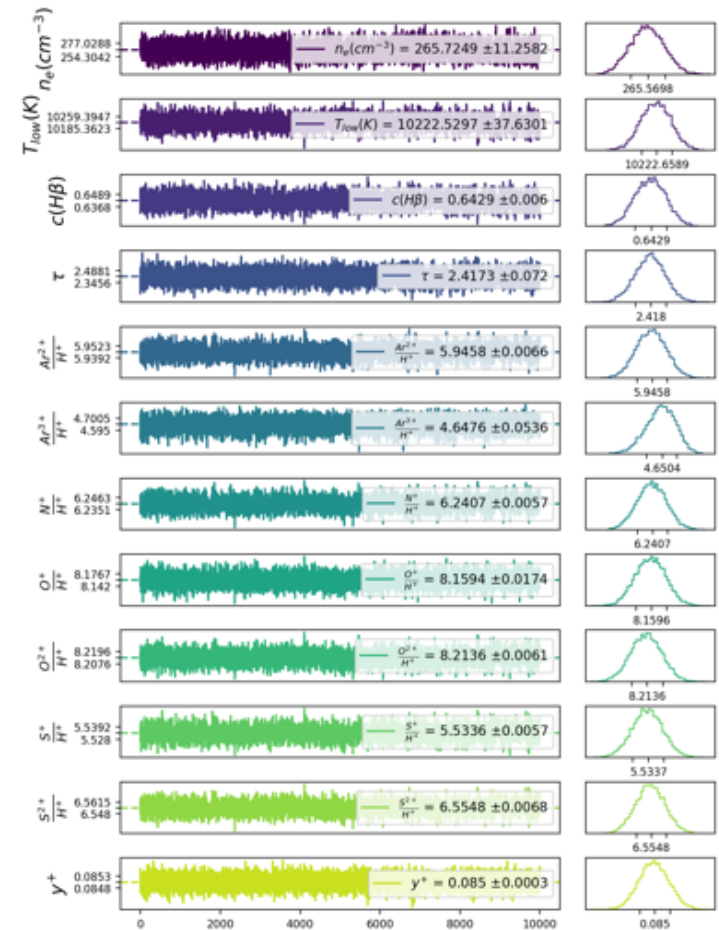




- We have introduced the derived methodology in the Bayesian algorithm described in Fernández et al. (2019).
- It simultaneously fits a 14 parameters chemical model, obtaining results which are fully compatible with those reported here

Parameter	True value	Mean	Standard deviation
$n_e(\text{cm}^{-3})$	None	265.7249	11.2582
$T_{\text{low}}(\text{K})$	None	10222.5297	37.6301
$\frac{A_{\text{r}^{2+}}}{H^+}$	None	5.9458	0.0066
$\frac{A_{\text{r}^{3+}}}{H^+}$	None	4.6476	0.0536
$\frac{N^+}{H^+}$	None	6.2407	0.0057
$\frac{O^+}{H^+}$	None	8.1594	0.0174
$\frac{O^{2+}}{H^+}$	None	8.2136	0.0061
$\frac{S^+}{H^+}$	None	5.5336	0.0057
$\frac{S^{2+}}{H^+}$	None	6.5548	0.0068
$c(H\beta)$	None	0.6429	0.006
$y^+$	None	0.085	$2.714e - 04$
$\tau$	None	2.4173	0.072

## Other codes





## Underlying stellar absorption

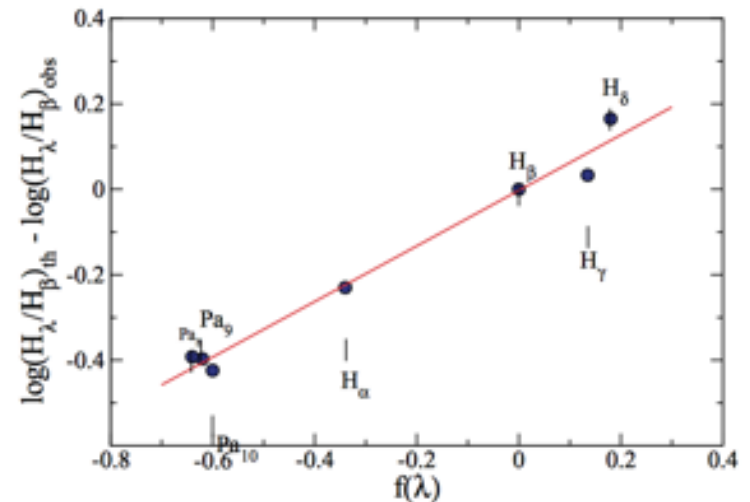
The underlying stellar absorption is less important than in the case of Helium.

### Helium lines:

- $EW(\text{He I } 4471) = 0.4 \text{ \AA}$   
(Izotov et al. 2007;  
González Delgado et al. 2005)
- $EW(\text{He I } 3889) / EW(\text{He I } 4471) = 1 \text{ \AA}$
- $EW(\text{He I } 5876) / EW(\text{He I } 4471) = 0.8 \text{ \AA}$   
(Leitherer et al. 1999; Izotov et al. 2010;  
González Delgado et al. 2005)
- $EW(\text{He I } 6678) / EW(\text{He I } 4471) = 0.4 \text{ \AA}$   
(Leitherer et al. 1999; Izotov et al. 2010)
- $EW(\text{He I } 7065) / EW(\text{He I } 4471) = 0.4 \text{ \AA}$

### Hydrogen lines:

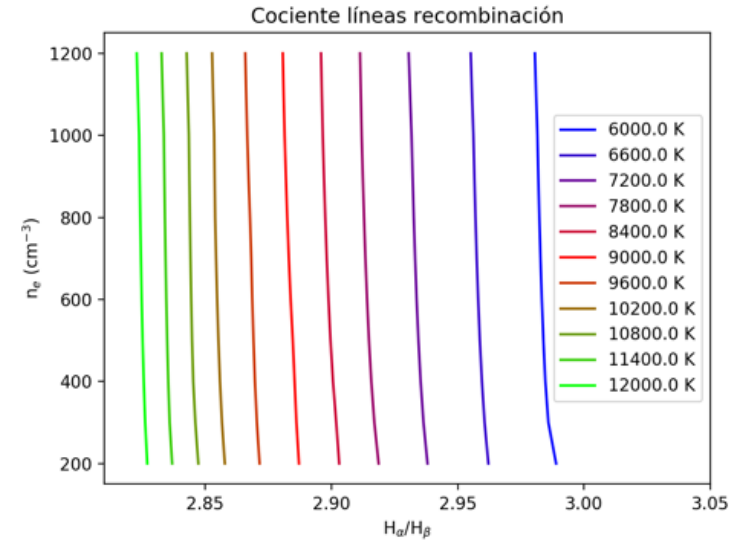
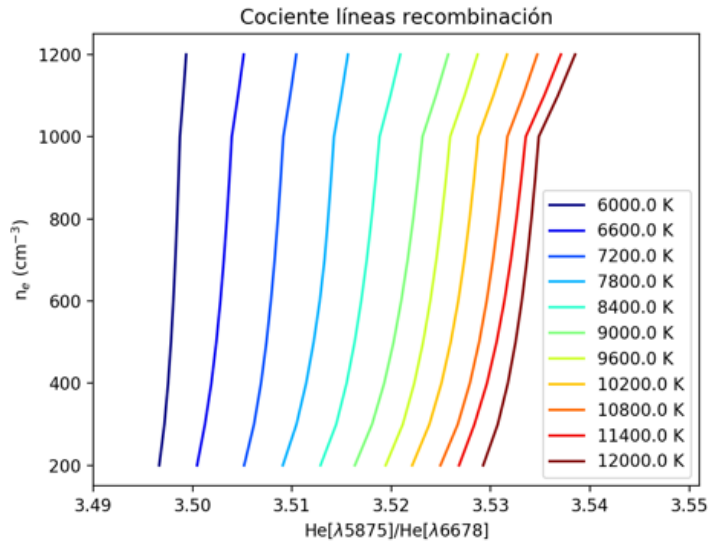
- $EW(\text{H}) = 2 \text{ \AA}$   
(McCall, Rybski & Shields 1985;  
Skillman & Kenicutt 1993)



Izotov et al. 1994.



## Temperatures and densities



- **Bootstrap model**  
Temperatures, 8000 K and 14000 K  
Densities, 50-500  $\text{cm}^{-3}$   
106 repeats, resampling with replacement  
PyNeb

$$\sigma(\text{H}) = 0.0185$$

$$\sigma(\text{He}) = 0.0041$$

The ratio of HeI lines are less affected by temperature and density variations.



## Conclusions

- 1- **Both methods** of extinction derivation, using H I or He I recombination lines, **are fully compatible** within the errors with each other and the errors in the determination of reddening constant get considerably reduced when both methods are used simultaneously.
- 2- **The results** presented in this work **will allow to study spatially resolved nebulae in their full extension**, analysing both high and low surface brightness regions simultaneously in a single moderate-to-long exposure pointing.
- 3- **We can recover saturated images from the archive** of different telescopes .
- 4- **We can determine interstellar extinction with** existing and coming up spectrographs that not includes Balmer lines.

**Thank you!**



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**May 19, 2022**